



Python in de klas

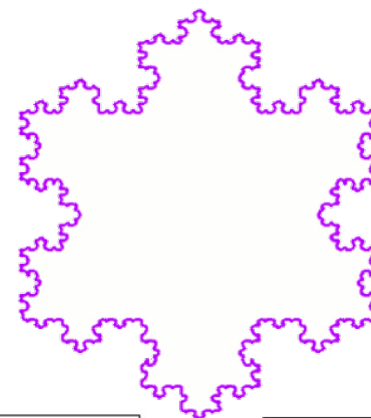
Koen Stulens – Bert Wikkerink



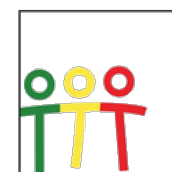
k-stulens@ti.com



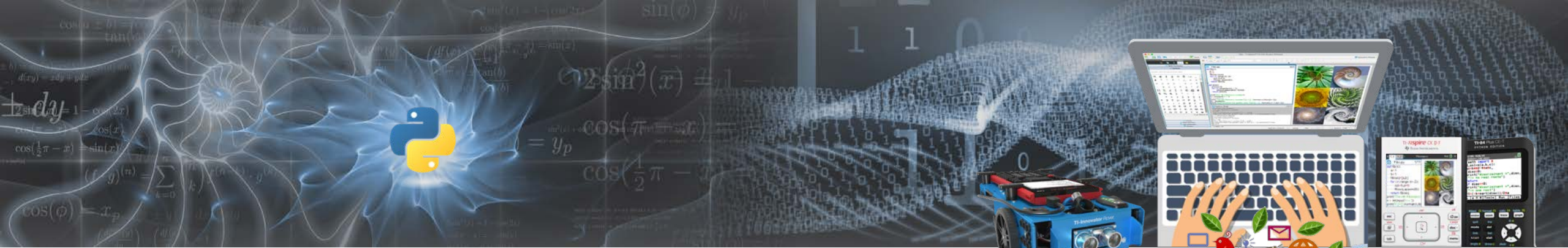
b.wikkerink@gmail.com



T³ NEDERLAND



T³ VLAANDEREN



Goesting in uitdagingen

1 Curiosity



- > Why? Explore!
- > Questions are windows to great instruction!

2 Embrace the mess



- > Try, Guess and Explore!
- > Learning is an inevitable process of trial & error

3 Reflection

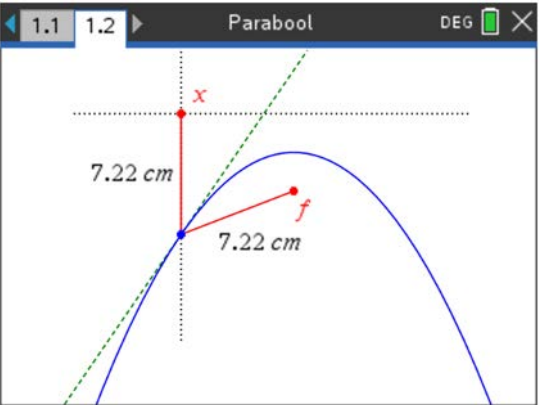
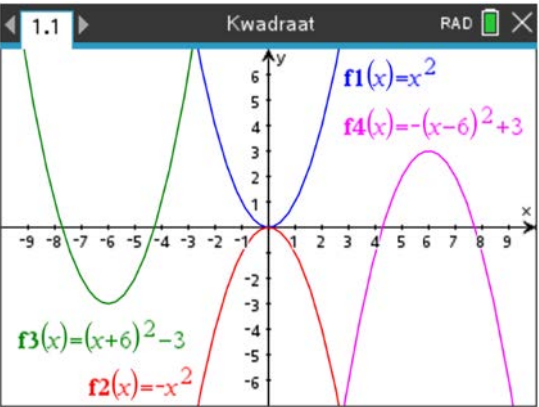


- > Teaching deserve revision
- > Learning needs revision



Representaties

Grafisch - Analytisch



Grafisch - Meetkundig

Tekst

1.1 1.2 Parabool RAD

Een parabool

is een vlakke tweedegraadskromme die de meetkundige plaats is van punten met dezelfde afstand tot een gegeven lijn, de richtlijn, en een gegeven punt, het brandpunt.

De wiskundige vergelijking die een parabool beschrijft, is van de tweede graad.

Numeriek

1.1 1.2 Kwadraat RAD

	A var	B func1	C func2	D func3
=		=f1(var)	=f2(var)	=f3(var)
1	-2	4	-4	13
2	-1	1	-1	22
3	0	0	0	33
4	1	1	-1	46
5	2	4	-4	61
A3	0			

1.1 1.2 1.3 Kwadraat RAD

Snijpunten

solve(f1(x)=0,x) ▶ x=0

solve(f3(x)=0,x) ▶ x=-(√3 +6) or x=√3 -6

Oplossen tweedegraadsvergelijkingen

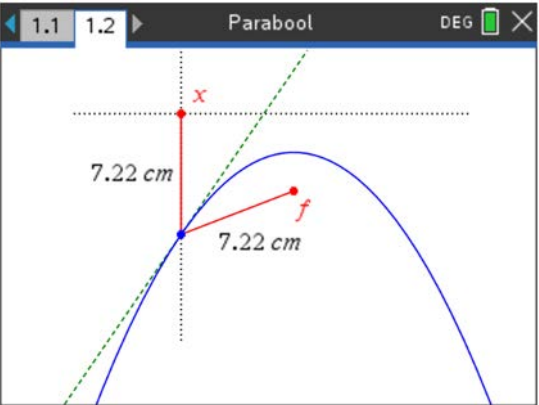
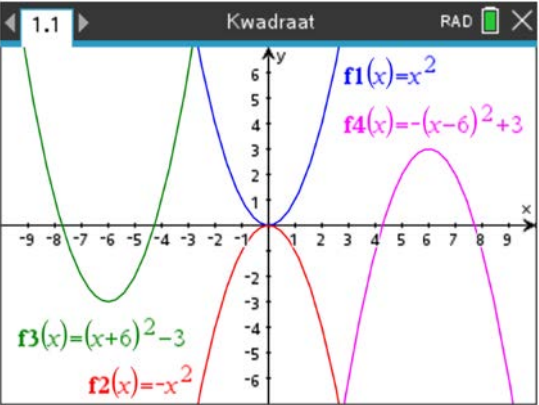
solve((x+6)^2-3=0,x) ▶ x=-(√3 +6) or x=√3 -6

solve(-(x-6)^2+3.=0,x) ▶ x=4.26795 or x=7.73205

Algebraïsch

Representaties

Grafisch - Analytisch



Grafisch - Meetkundig

Tekst

1.1 1.2 Parabool RAD

Een parabool

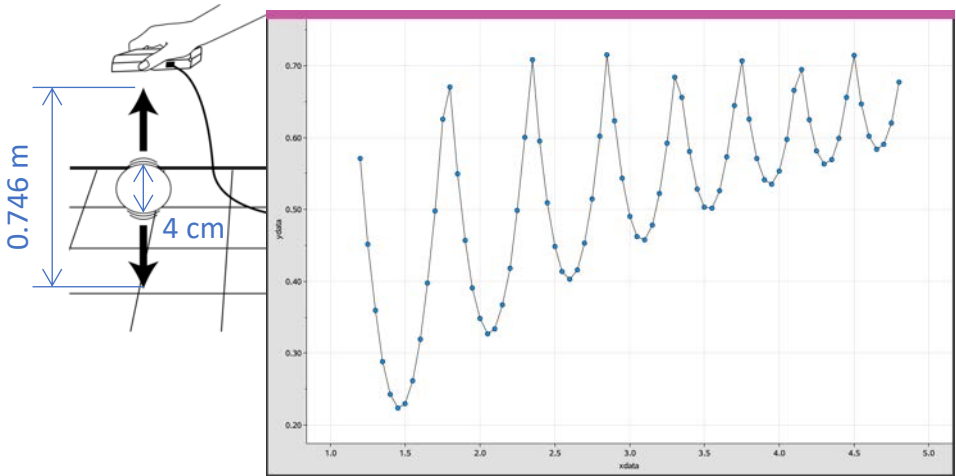
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A3	0			

Modelleren



1.1 1.2 1.3 Kwadraat RAD

Snijpunten

$\text{solve}(f1(x)=0,x) \rightarrow x=0$

$\text{solve}(f3(x)=0,x) \rightarrow x=-(\sqrt{3}+6) \text{ or } x=\sqrt{3}-6$

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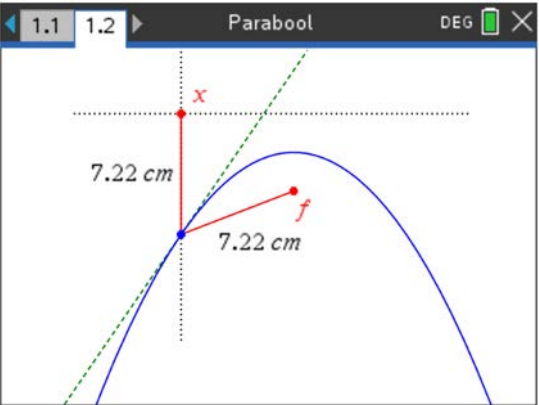
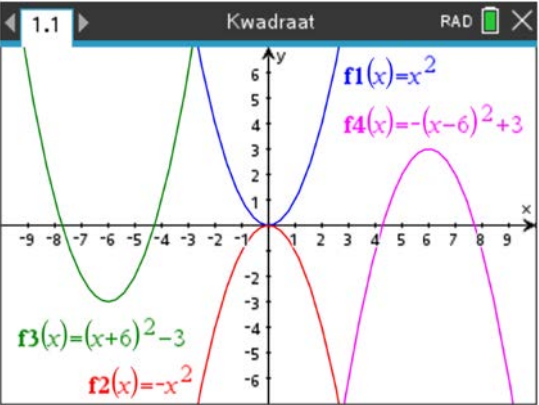
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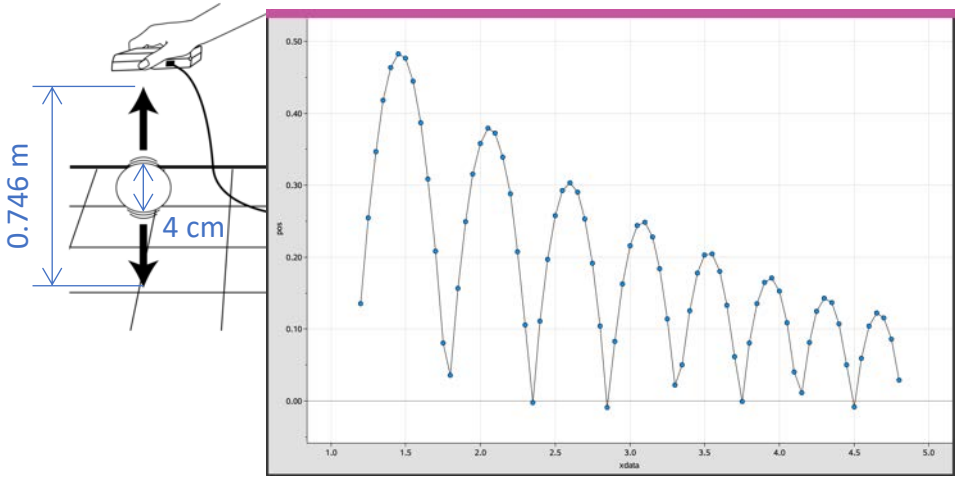
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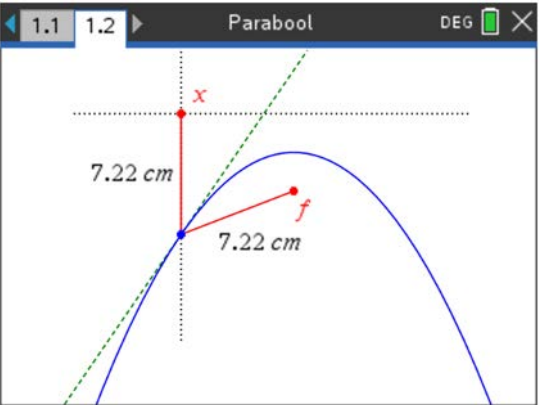
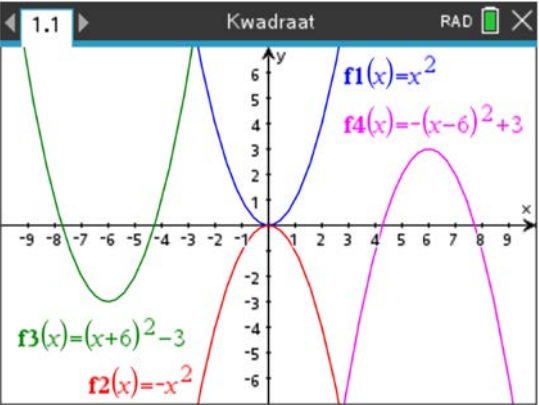
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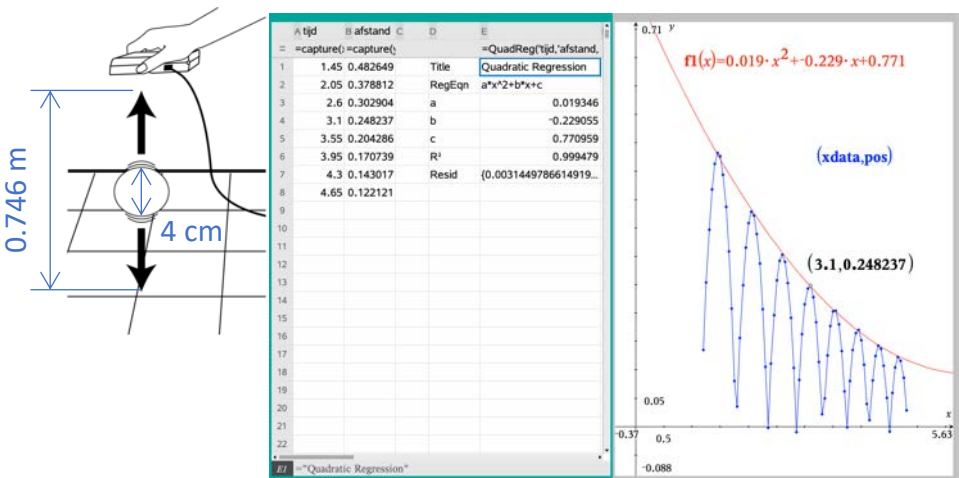
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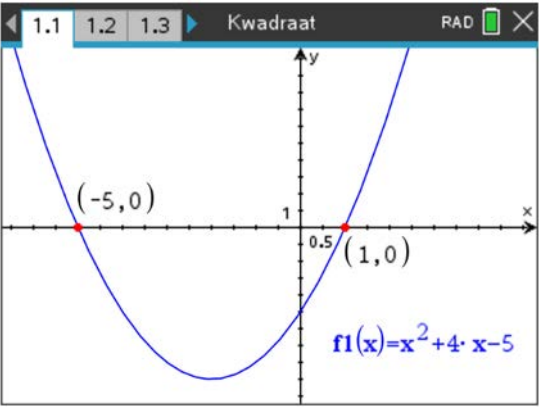
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Numeriek

	1.1	1.2	1.3 ▸ Kwadraat RAD
x	f1(x):=	f2(x):=	
	x^2+4x-5	$-x^2$	
-5.	0.	-25.	
-4.	-5.	-16.	
-3.	-8.	-9.	
-2.	-9.	-4.	
-1.	-8.	-1.	
0.			

Programmeren

```
Q SOLVE.py
from math import *
def qsolve(a,b,c):
    d=b**2-4*a*c
    if d>0:
        print("D =",d,">> two roots")
        r1=(-b-sqrt(d))/2*a
        r2=(-b+sqrt(d))/2*a
        return r1,r2
    elif d==0:
        print("D =",d,">> one root")
        r1=-b/2*a
        return r1
    else:
        print("D =",d,">> no real roots")
    return
```

1.1 ▸ Quadratic RAD

Quadratic Functions

Q SOLVE.py 1/15

```
from math import *
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        return r1,r2
```

Python Shell 6/6

```
>>>#Running QSOLV
>>>from QSOLVE im
>>>qsolve(1,4,-5)
D = 36 >> two roots
(-5.0, 1.0)
>>>|
```



1.3 1.4 1.5 ▸ *Kwadraat RAD

Snijpunten

solve(f1(x)=0,x) • x=-5 or x=1

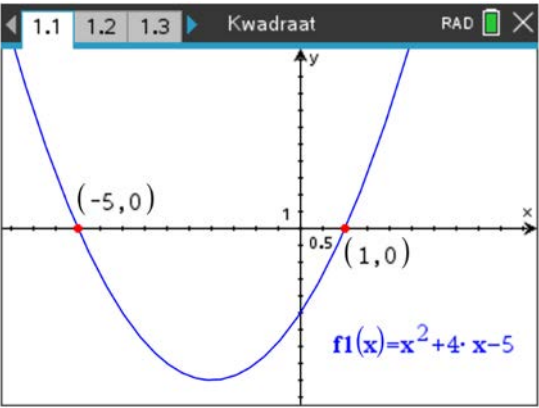
Oplossen tweedegraadsvergelijking

solve(x^2+4x-5=0,x) • x=-5 or x=1

Algebraïsch

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    return
```

www.t3nederland.nl/nl/t3-europe/edublogs

Ik hoop dat leerlingen
zo enthousiast worden
dat ze Python ook
buiten schooltijd gaan
gebruiken!



1.3 1.4 1.5 ▸ *Kwadraat RAD

Snijpunten

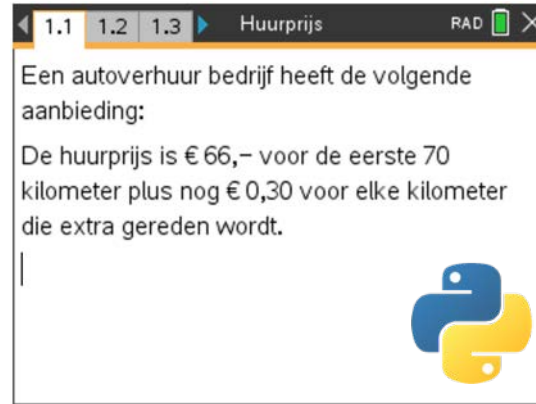
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Oplossen tweedegraadsvergelijking

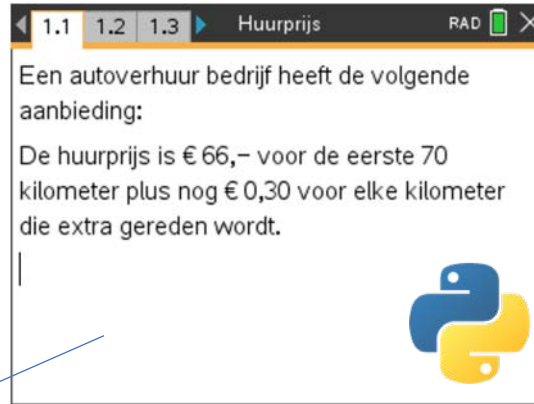
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Algebraïsch

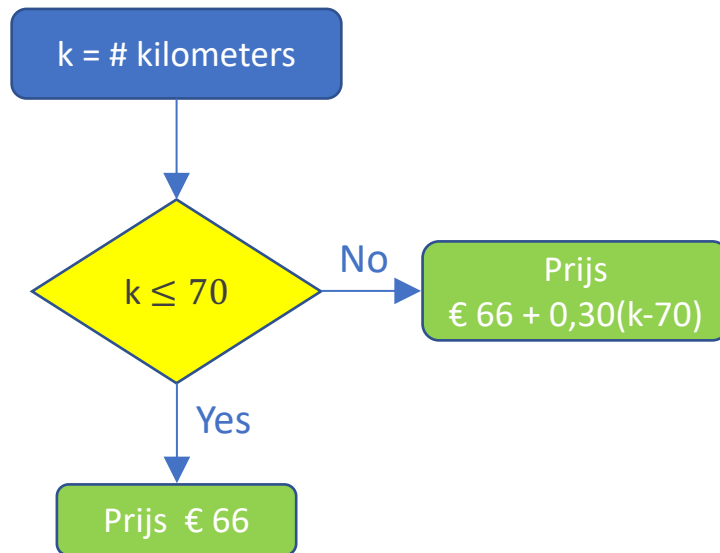
Programmeren



Programmeren



Analyseren

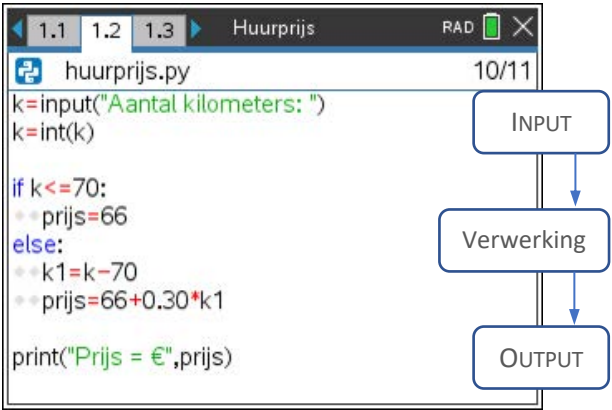
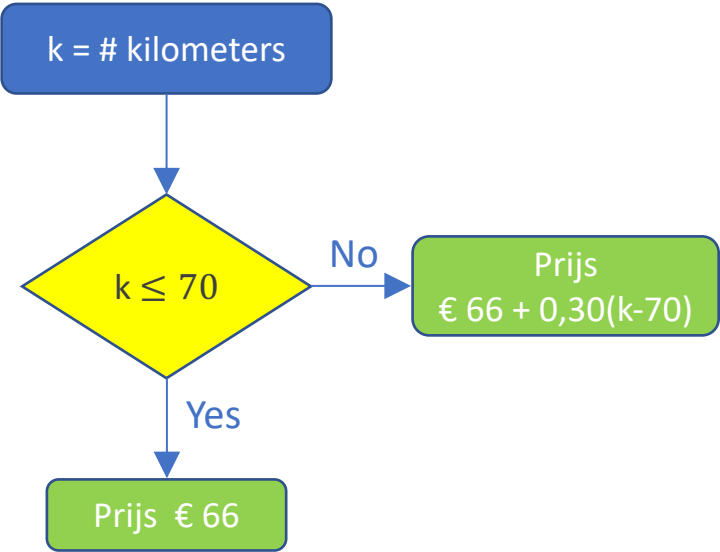


Programmeren



Analyseren

Vertalen



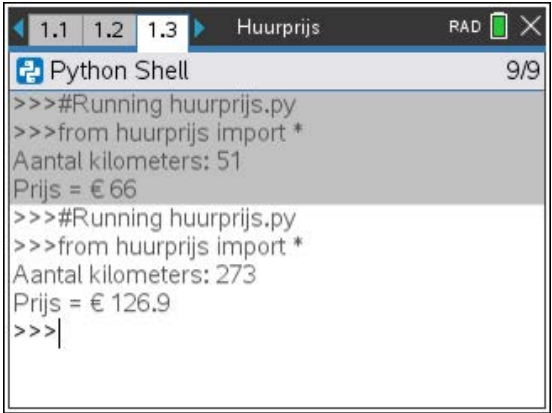
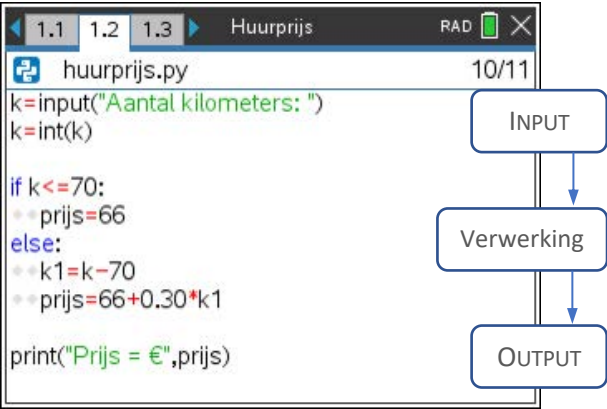
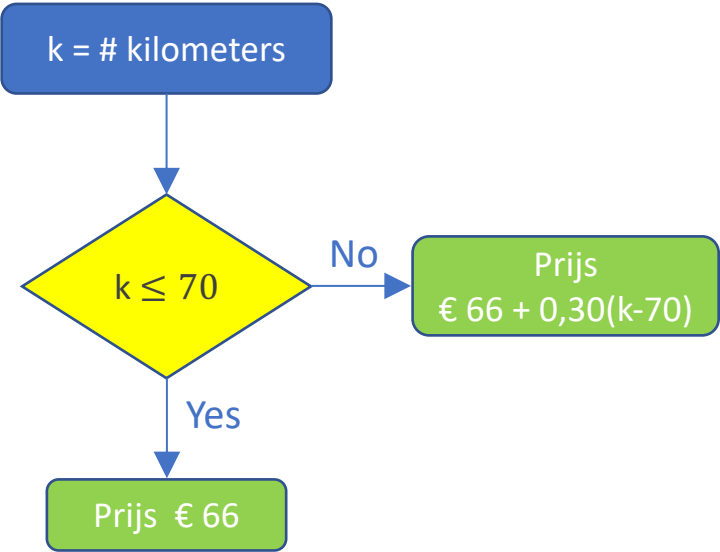
Programmeren



Analyseren

Vertalen

Verwerking



Programmeren

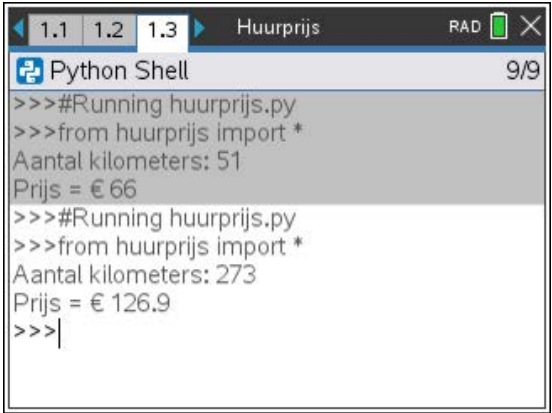
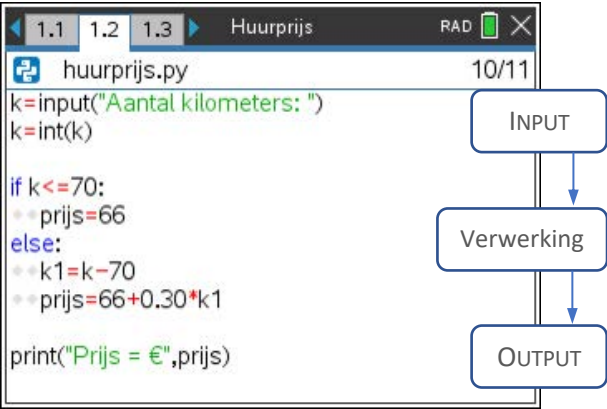
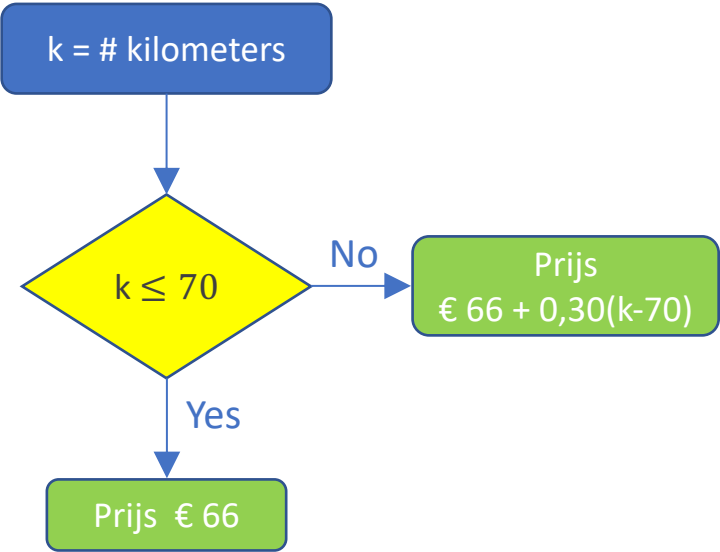


Controle

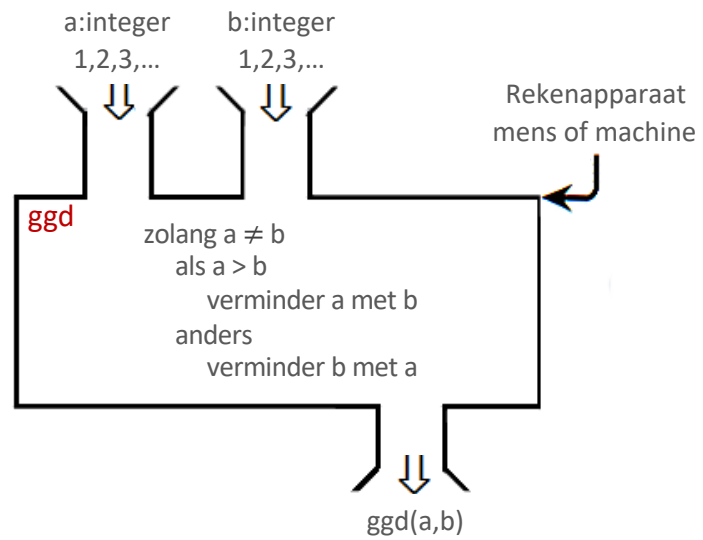
Analyseren

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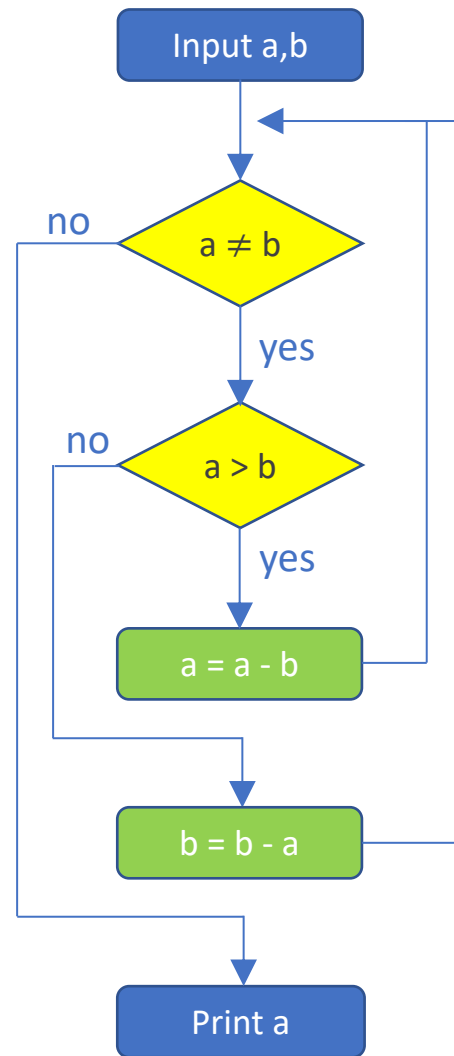
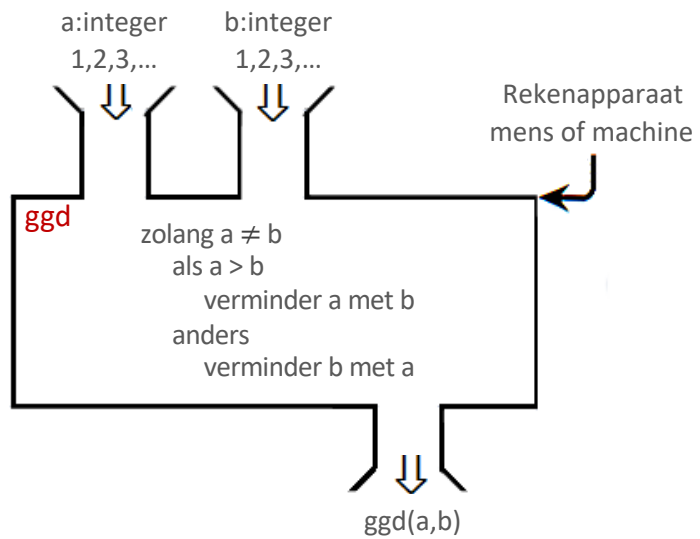
Verwerking



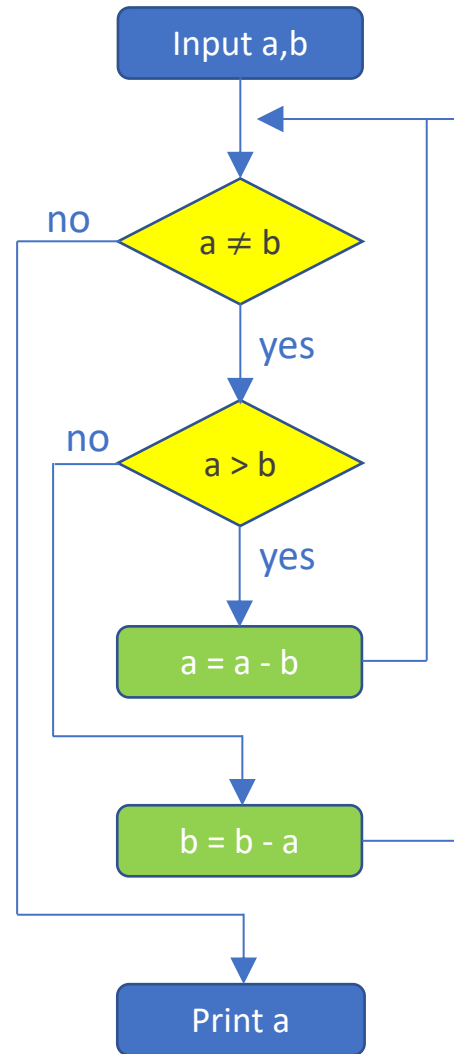
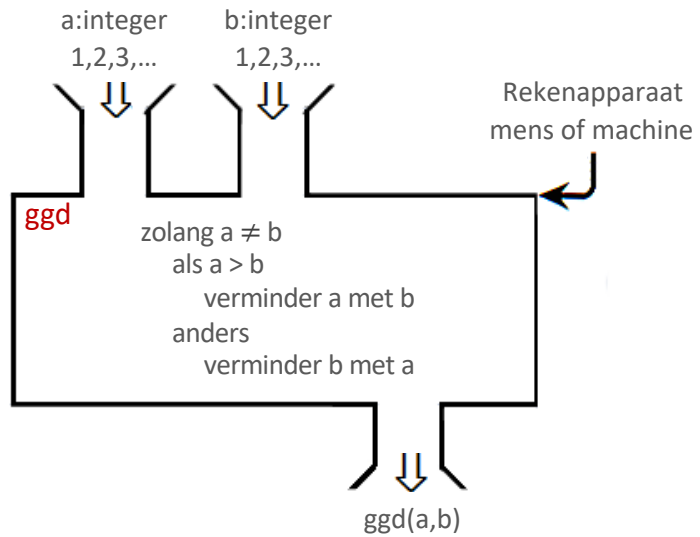
Algoritme van Euclides



Algoritme van Euclides



Algoritme van Euclides



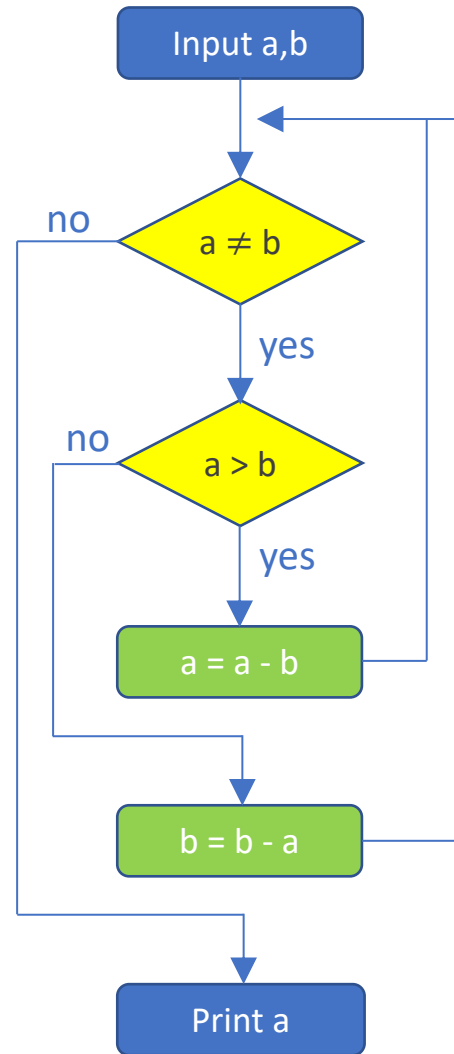
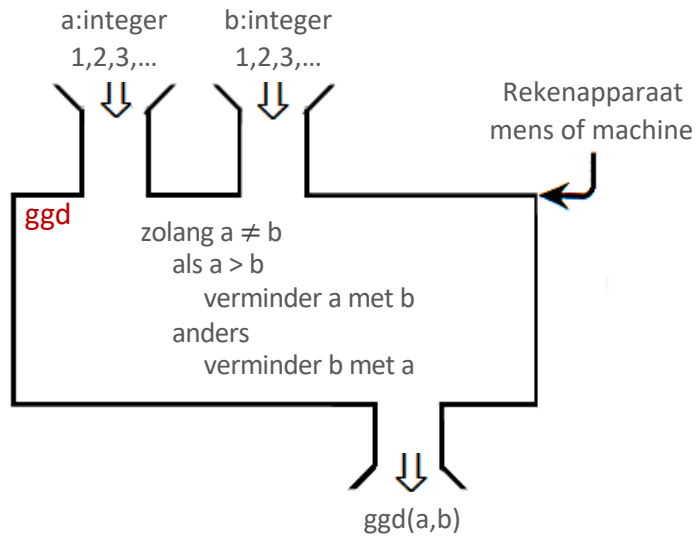
ggd.py

```
a=int(input("a= "))
b=int(input("b= "))

while a!=b:
    if a>b:
        a=a-b
    else:
        b=b-a

print(a)
```

Algoritme van Euclides



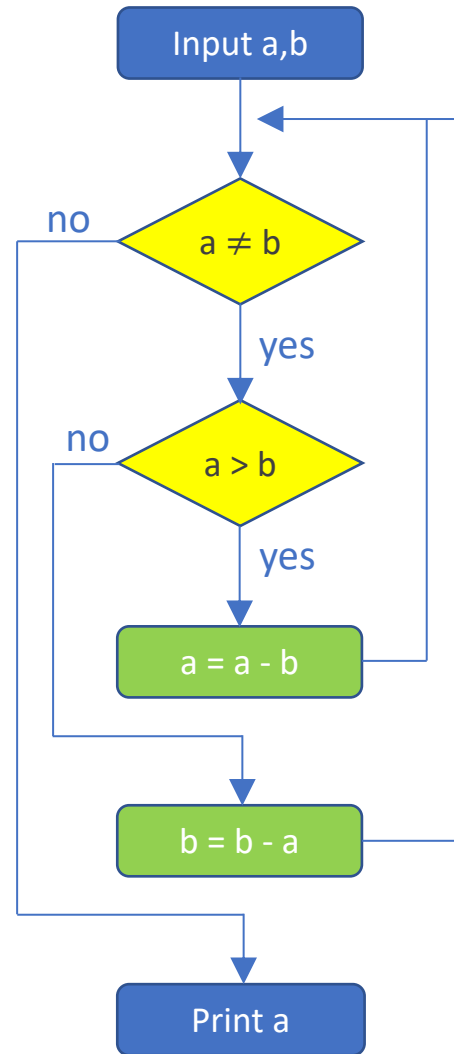
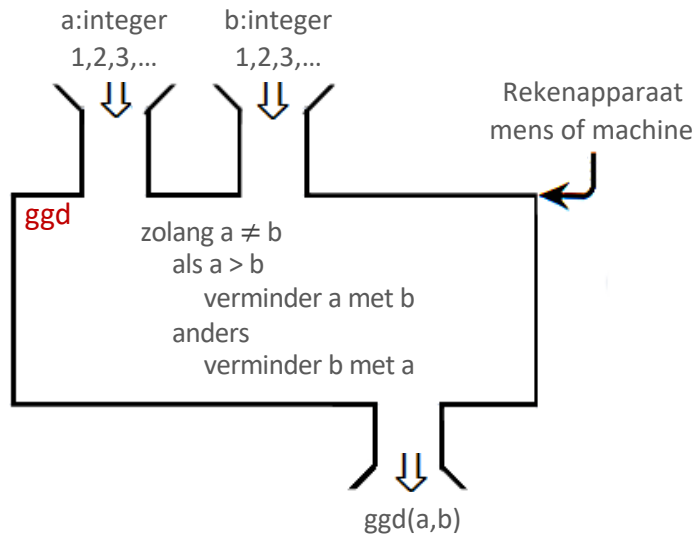
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Python Shell
>>>#Running ggd.py
>>>from ggd import *
a= 48
b= 36
12
>>>
```


Algoritme van Euclides



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a=int(input("a= "))
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ggd.py

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a=int(input("a= "))
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```
x,y = a,b
```

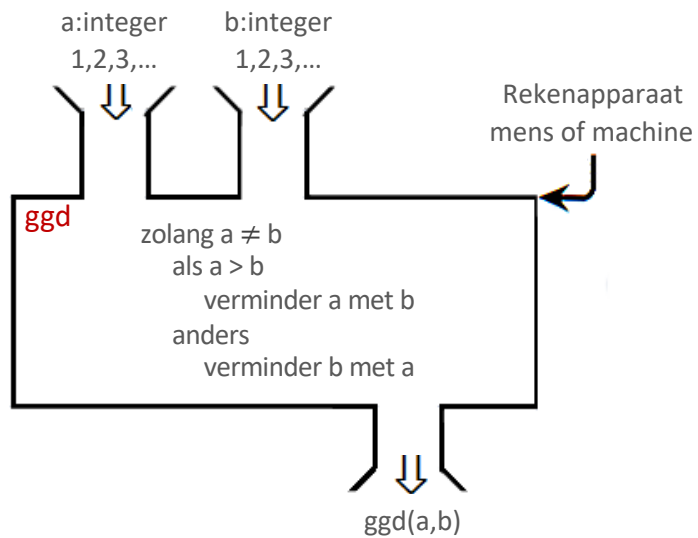
```
while x!=y:
    if x>y:
        x=x-y
    else:
        y=y-x
```

```
print("De grootste gemene deler van {} en {} = {}".format(a,b,x))
```

Python Shell

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>>>#Running ggd.py
>>>from ggd import *
a= 48
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De grootste gemene deler van 48 en 36 = 12
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Algoritme van Euclides

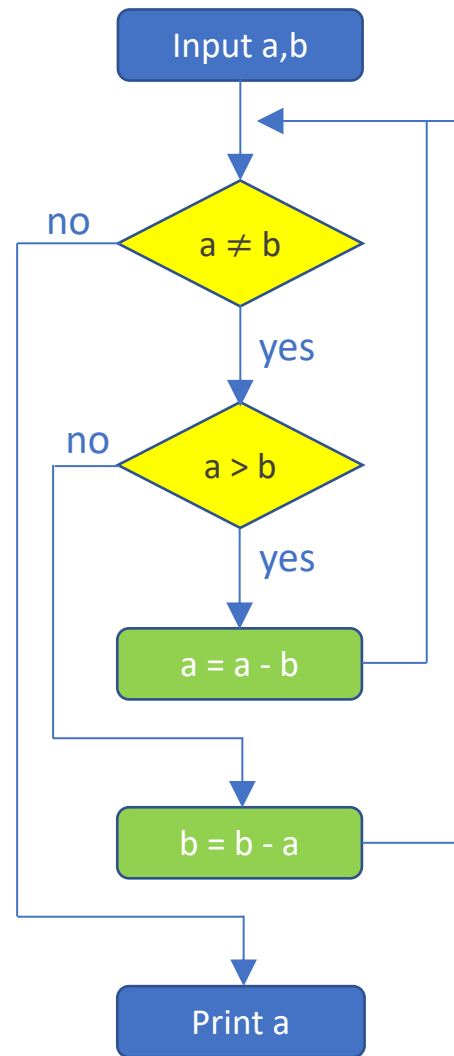


ggd.py

```
def ggd(a,b):  
    while a!=b:  
        if a>b:  
            a=a-b  
        else:  
            b=b-a  
    return a
```

Python Shell

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>>>from ggd import *  
>>>ggd(48,36)  
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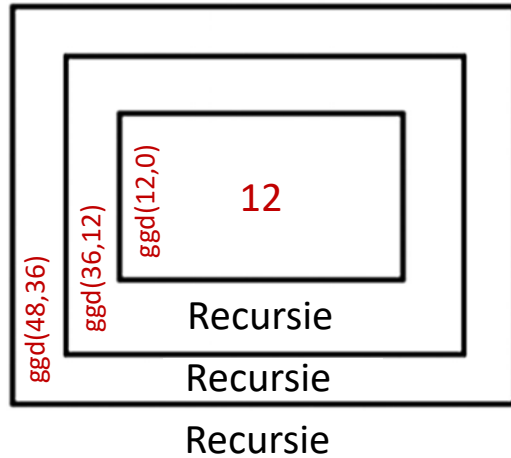
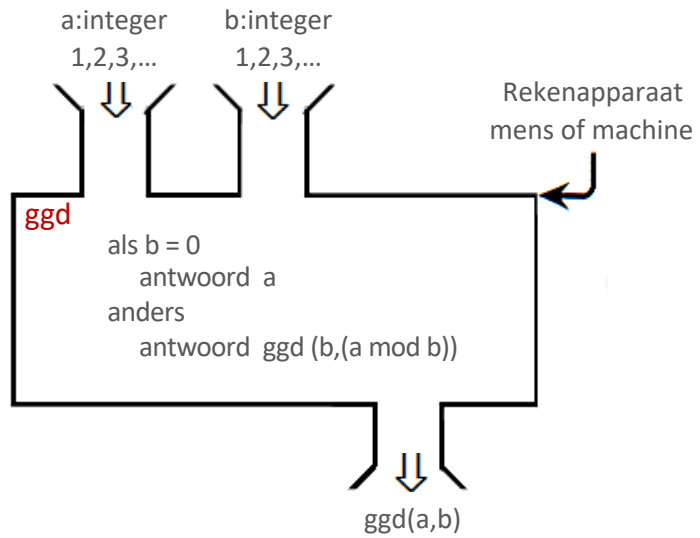
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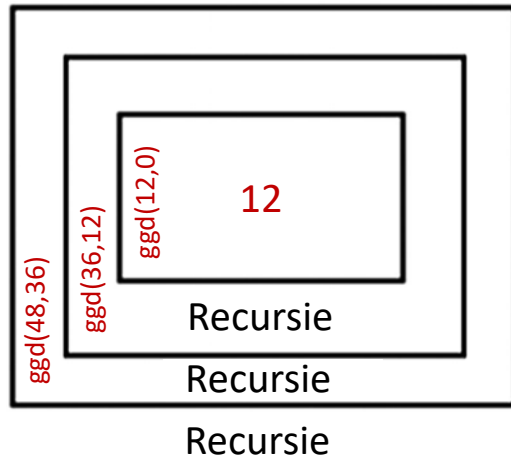
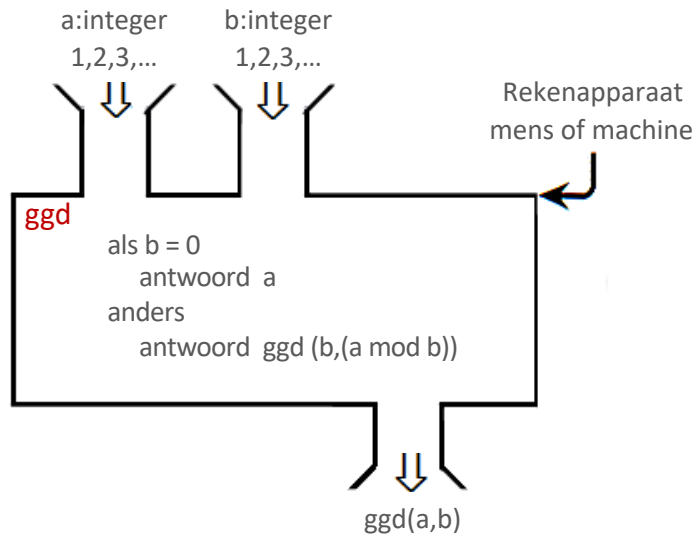
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a= 48  
b= 36  
De grootste gemene deler van 48 en 36 = 12  
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```

Algoritme van Euclides



Algoritme van Euclides



`ggd.py`

```
a=int(input("a= "))
b=int (input("b= " ))
```

```
def ggd(p,q):
    if q==0:
        return p
    else:
        return ggd(q,p%q)
```

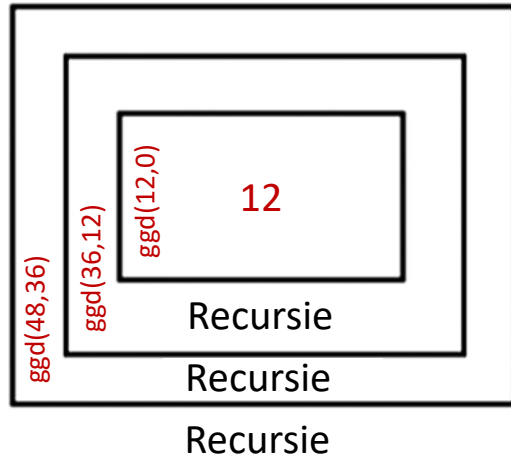
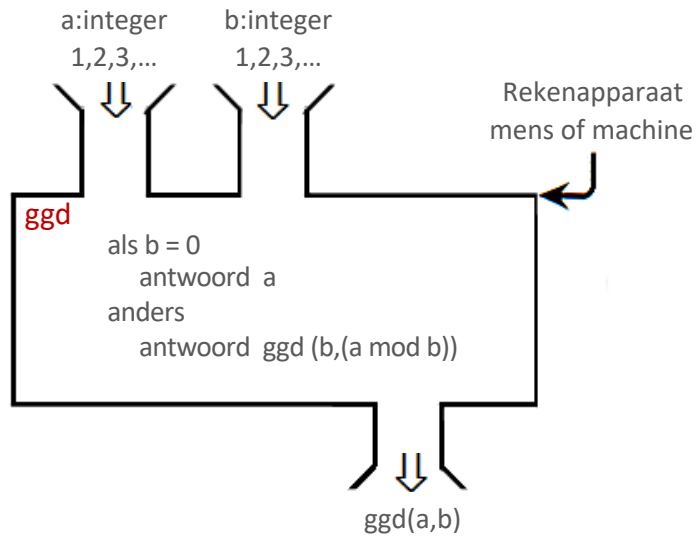
```
c=ggd(a,b)
```

```
print("De grootste gemene deler van {} en {} = {}".format(a,b,c))
```

Python Shell

```
>>>#Running ggd.py
>>>from ggd import *
a= 48
b= 36
De grootste gemene deler van 48 en 36 = 12
>>>
```

Algoritme van Euclides



 **ggd.py**

```
a=int(input("a= "))
b=int (input("b= " ))
```

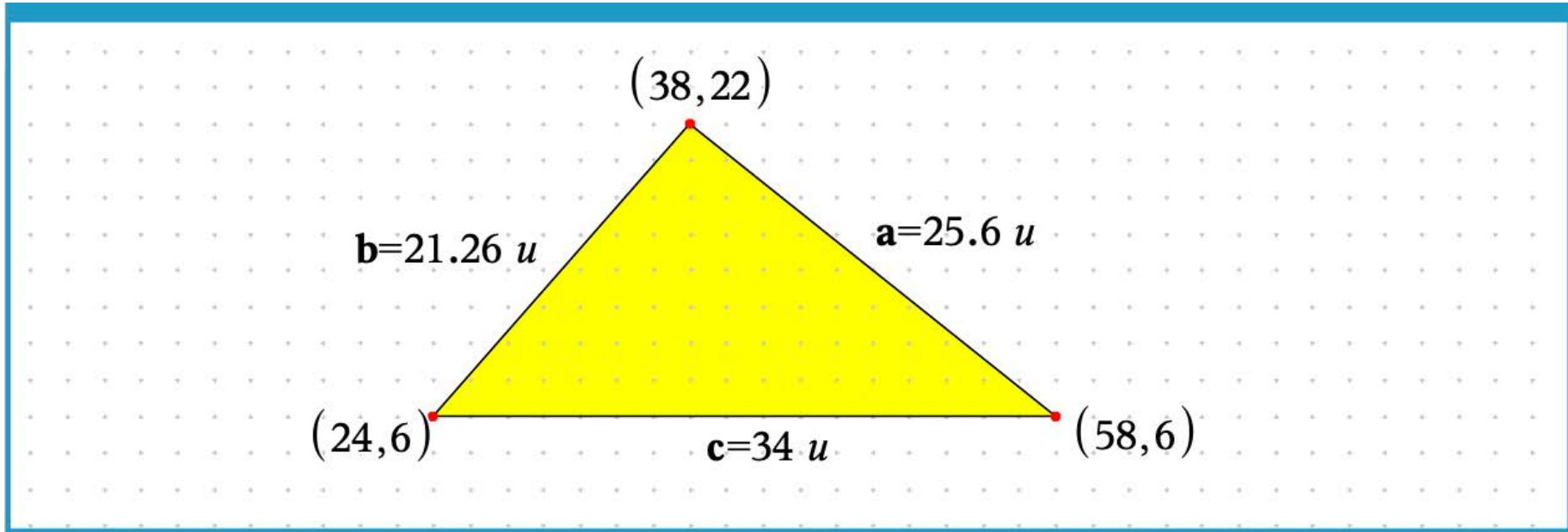
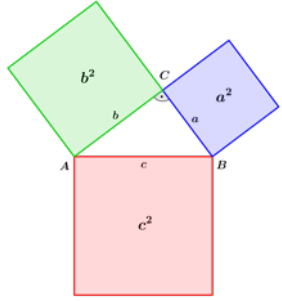
```
def ggd(p,q):
    if q==0:
        return p
    else:
        return ggd(q,p%q)
```

```
print("De grootste gemene deler van {} en {} = {}".format(a,b,ggd(a,b)))
```

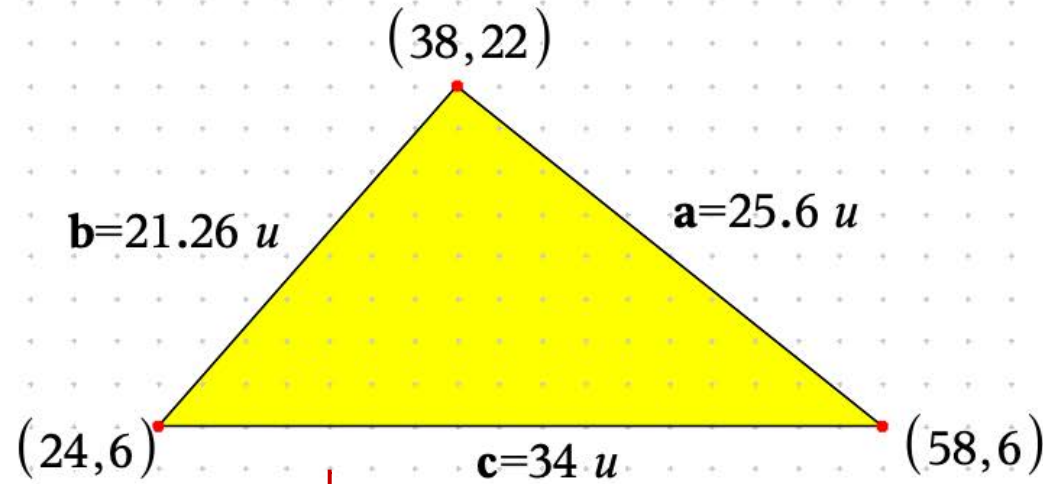
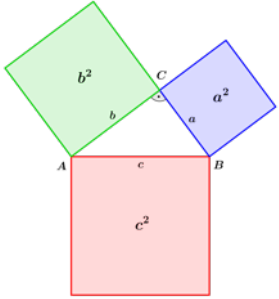
 **Python Shell**

```
>>>#Running ggd.py
>>>from ggd import *
a= 48
b= 36
De grootste gemene deler van 48 en 36 = 12
>>>
```

Pythagoras



Pythagoras



Pythagoras.py

14/14

Python Shell

4/4

```
from ti_system import *
```

```
L=[0]*3
```

```
L[0]=recall_value("a")
```

```
L[1]=recall_value("b")
```

```
L[2]=recall_value("c")
```

```
L.sort()
```

```
a=round(float(L[0]),2)
```

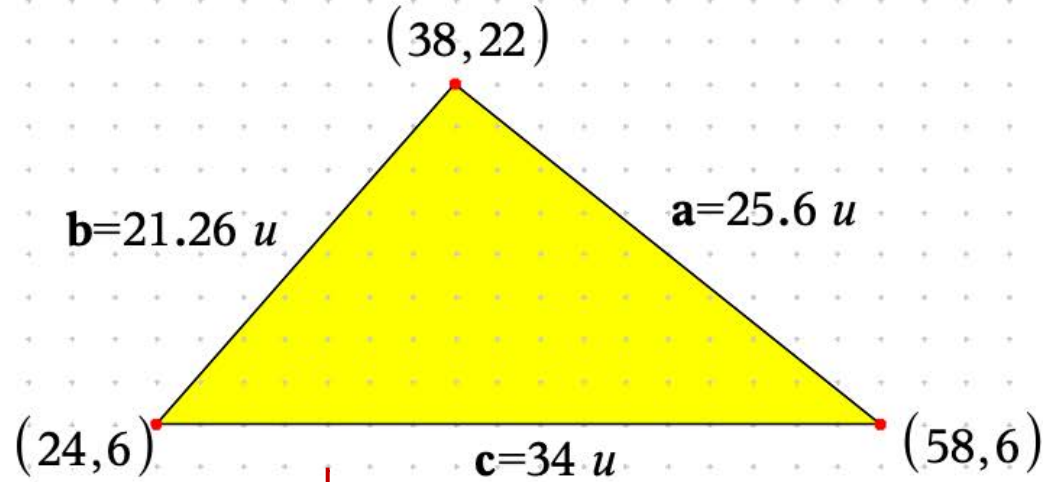
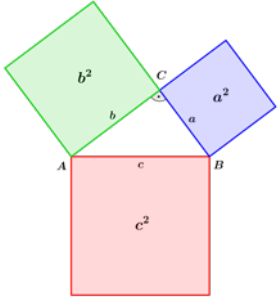
```
b=round(float(L[1]),2)
```

```
c=round(float(L[2]),2)
```

```
print("De driehoek ∠ {0} , {1} , {2}".format(a,b,c))
```

Variabelen uitwisselen

Pythagoras



Pythagoras.py

14/14

Python Shell

4/4

```
from ti_system import *
```

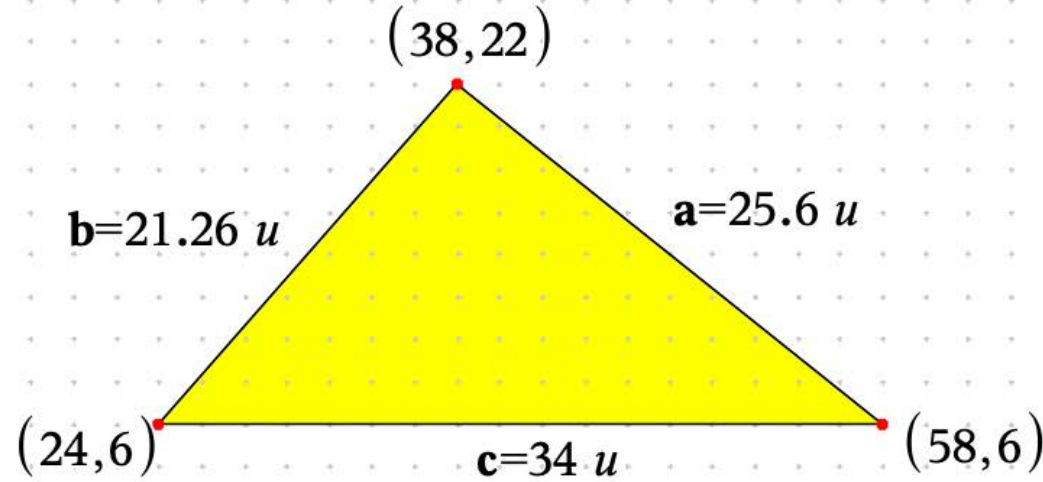
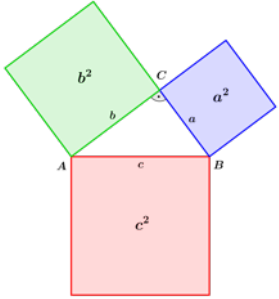
```
L=[0]*3  
L[0]=recall_value("a")  
L[1]=recall_value("b")  
L[2]=recall_value("c")  
L.sort()
```

Variabelen uitwisselen

```
a=round(float(L[0]),2)  
b=round(float(L[1]),2)  
c=round(float(L[2]),2)  
print("De driehoek ∠ { } , { } , { } ".format(a,b,c))
```

```
>>>#Running Pythagoras.py  
>>>from Pythagoras import *  
De driehoek ∠ 21.26 , 25.61 , 34.0  
>>>
```

Pythagoras



Pythagoras.py

16/16

```
from ti_system import *
```

```
L=[0]*3
L[0]=recall_value("a");L[1]=recall_value("b");L[2]=recall_value("c")
L.sort()
```

```
a=round(float(L[0]),2)
b=round(float(L[1]),2)
c=round(float(L[2]),2)
print("De driehoek ∠ {0} , {1} , {2} ".format(a,b,c))
```

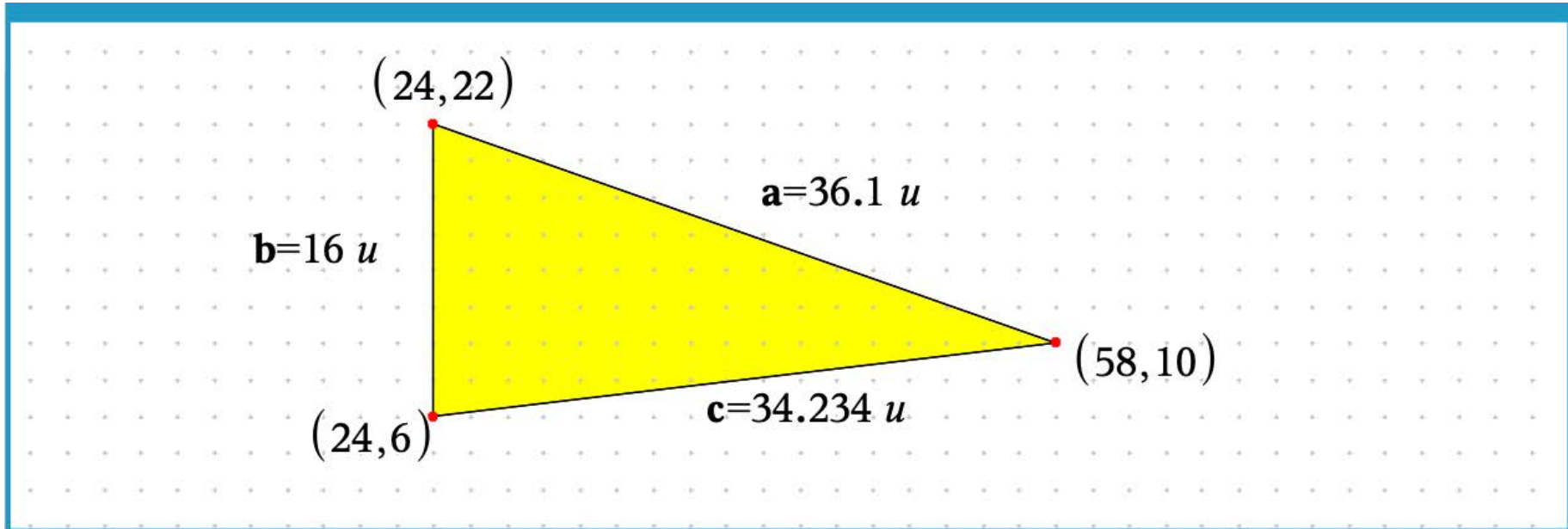
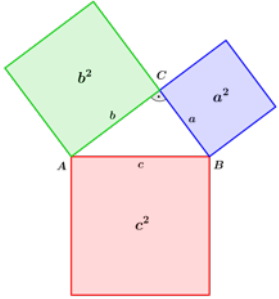
```
if round(L[2]**2/(L[0]**2+L[1]**2),4)==1:
    print("is een rechthoekige driehoek")
else:
    print("is geen rechthoekige driehoek")
|
```

Python Shell

8/8

```
>>>#Running Pythagoras.py
>>>from Pythagoras import *
De driehoek ∠ 21.26 , 25.61 , 34.0
>>>#Running Pythagoras.py
>>>from Pythagoras import *
De driehoek ∠ 21.26 , 25.61 , 34.0
is geen rechthoekige driehoek
>>>|
```

Pythagoras



Pythagoras.py

11/16

```
from ti_system import *
```

```
L=[0]*3  
L[0]=recall_value("a");L[1]=recall_value("b");L[2]=recall_value("c")  
L.sort()
```

```
a=round(float(L[0]),2)  
b=round(float(L[1]),2)  
c=round(float(L[2]),2)  
print("De driehoek ∠ {}, {}, {}".format(a,b,c))
```

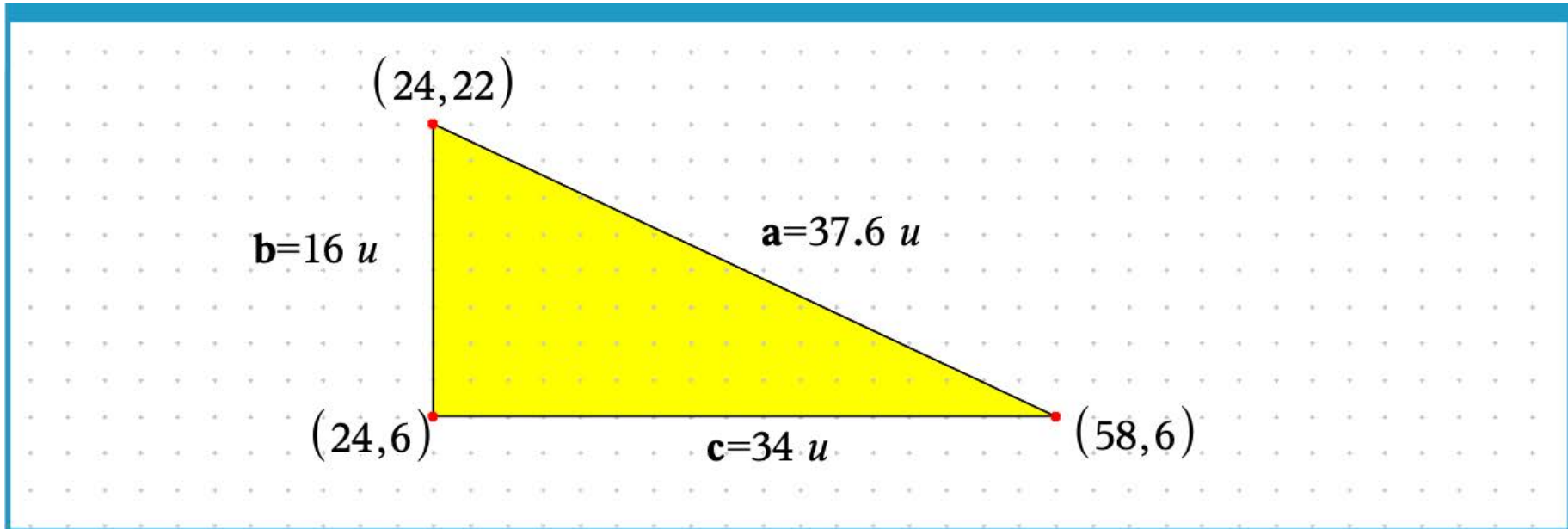
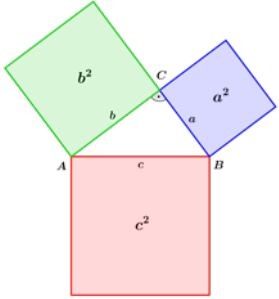
```
if round(L[2]**2/(L[0]**2+L[1]**2),4)==1:  
    print("is een rechthoekige driehoek")  
else:  
    print("is geen rechthoekige driehoek")
```

Python Shell

12/12

```
>>>#Running Pythagoras.py  
>>>from Pythagoras import *  
De driehoek ∠ 21.26 , 25.61 , 34.0  
>>>#Running Pythagoras.py  
>>>from Pythagoras import *  
De driehoek ∠ 21.26 , 25.61 , 34.0  
is geen rechthoekige driehoek  
>>>#Running Pythagoras.py  
>>>from Pythagoras import *  
De driehoek ∠ 16.0 , 34.23 , 36.06  
is geen rechthoekige driehoek  
>>>
```

Pythagoras



Pythagoras.py

13/16

```
from ti_system import *
```

```
L=[0]*3
```

```
L[0]=recall_value("a");L[1]=recall_value("b");L[2]=recall_value("c")
```

```
L.sort()
```

```
a=round(float(L[0]),2)
```

```
b=round(float(L[1]),2)
```

```
c=round(float(L[2]),2)
```

```
print("De driehoek ∠ {}, {}, {}".format(a,b,c))
```

```
if round(L[2]**2/(L[0]**2+L[1]**2),4)==1:
```

```
    print("is een rechthoekige driehoek")
```

```
else:
```

```
    print("is geen rechthoekige driehoek")
```

Python Shell

16/16

```
>>>#Running Pythagoras.py
```

```
>>>from Pythagoras import *
```

```
De driehoek ∠ 21.26 , 25.61 , 34.0
```

```
>>>#Running Pythagoras.py
```

```
>>>from Pythagoras import *
```

```
De driehoek ∠ 21.26 , 25.61 , 34.0
```

```
is geen rechthoekige driehoek
```

```
>>>#Running Pythagoras.py
```

```
>>>from Pythagoras import *
```

```
De driehoek ∠ 16.0 , 34.23 , 36.06
```

```
is geen rechthoekige driehoek
```

```
>>>#Running Pythagoras.py
```

```
>>>from Pythagoras import *
```

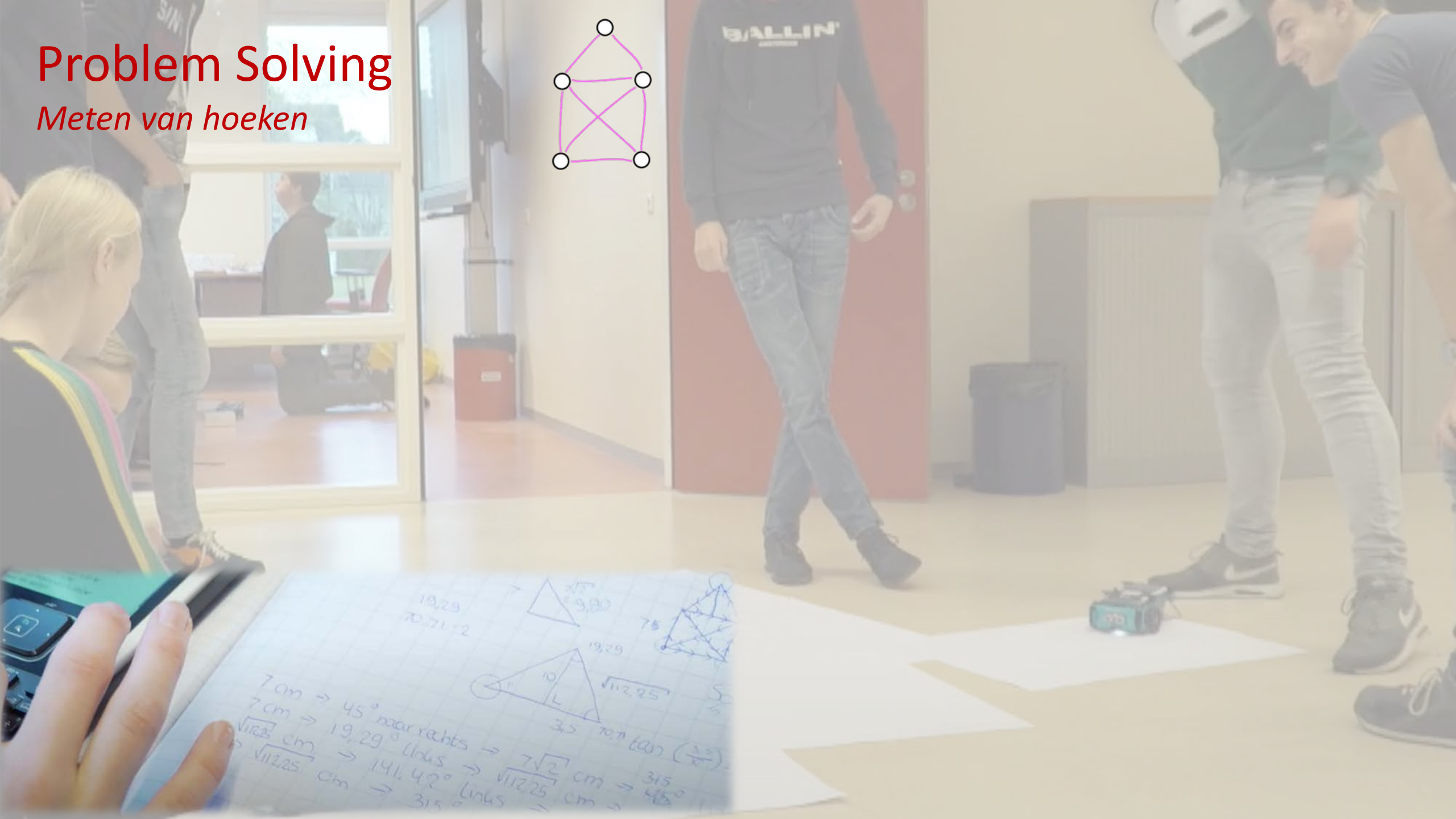
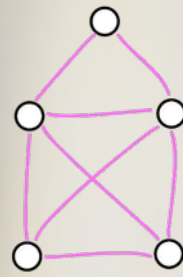
```
De driehoek ∠ 16.0 , 34.0 , 37.58
```

```
is een rechthoekige driehoek
```

```
>>>
```


Problem Solving

Meten van hoeken



Handwritten calculations and diagrams on graph paper:

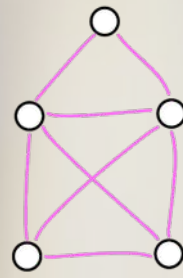
19,29
70,7112

7 cm $\rightarrow 45^\circ$ naar rechts $\rightarrow 7\sqrt{2}$ cm $\rightarrow 315^\circ$
7 cm $\rightarrow 19,29^\circ$ links $\rightarrow \sqrt{112,25}$ cm $\rightarrow 45^\circ$
 $\sqrt{112,25}$ cm $\rightarrow 141,42^\circ$ links $\rightarrow 315^\circ$

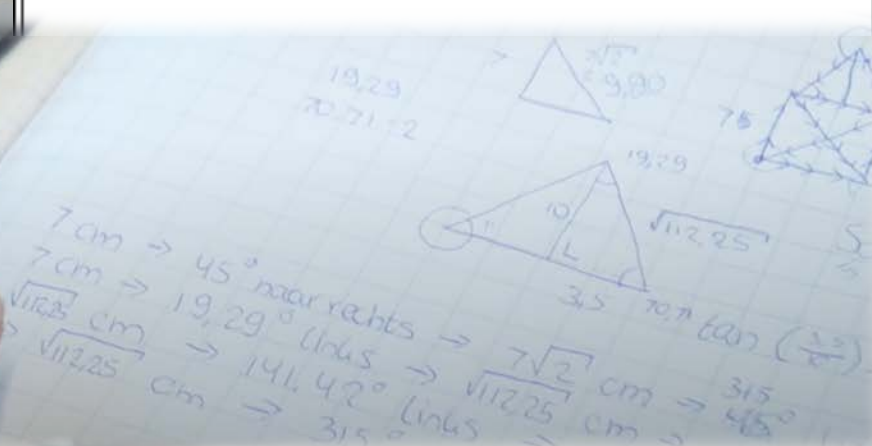
Diagrams include a right triangle with sides 7 and 7, a larger triangle with sides 10 and 3,5, and a complex geometric construction with multiple lines and angles.

Problem Solving

Meten van hoeken

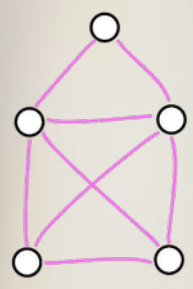


```
1.1 1.2 Rover RAD    
rover.py 8/11  
import ti_rover as rv  
rv.forward(3)
```



Problem Solving

Meten van hoeken



```
1.1 1.2 Rover RAD  
rover.py 8/8
import ti_rover as rv

for i in range(4):
    rv.forward(3)
    rv.right(90)
```



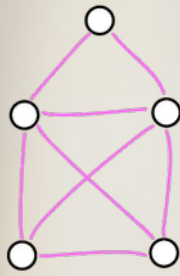
Handwritten calculations and diagrams on a piece of paper. The calculations include:

- $7\text{ cm} \rightarrow 45^\circ$ naar rechts $\rightarrow 7\sqrt{2}\text{ cm} \rightarrow 315^\circ$
- $7\text{ cm} \rightarrow 19,29^\circ$ links $\rightarrow \sqrt{112,25}\text{ cm} \rightarrow 45^\circ$
- $\sqrt{112,25}\text{ cm} \rightarrow 141,42^\circ$ links $\rightarrow 315^\circ$

The diagrams include a right-angled triangle with a hypotenuse of 10 and a leg of 7 , and a larger triangle with a hypotenuse of 10 and a leg of $3,5$.

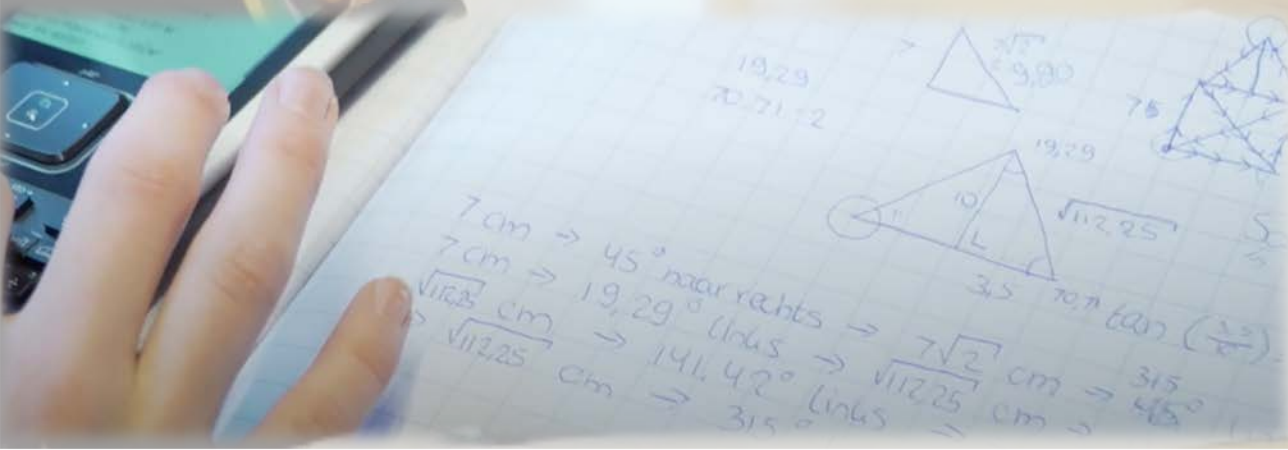
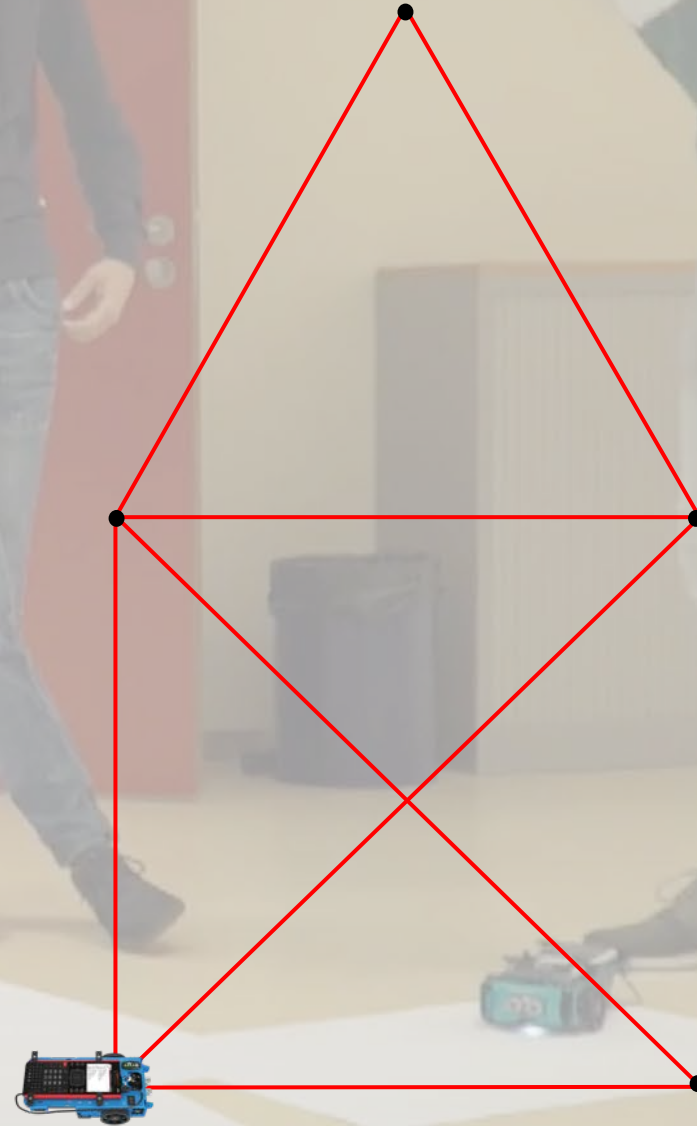
Problem Solving

Meten van hoeken



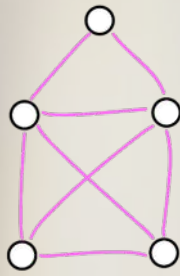
```
import ti_rover as rv
rv.forward(a)
rv.left(90)
rv.forward(a)
rv.left(90)
rv.forward(a)
rv.right(120)
rv.forward(a)

rv.right(120)
rv.forward(a)
rv.right(75)
rv.forward(sqrt(2)*a)
rv.right(135)
rv.forward(sqrt(2)*a)
```



Problem Solving

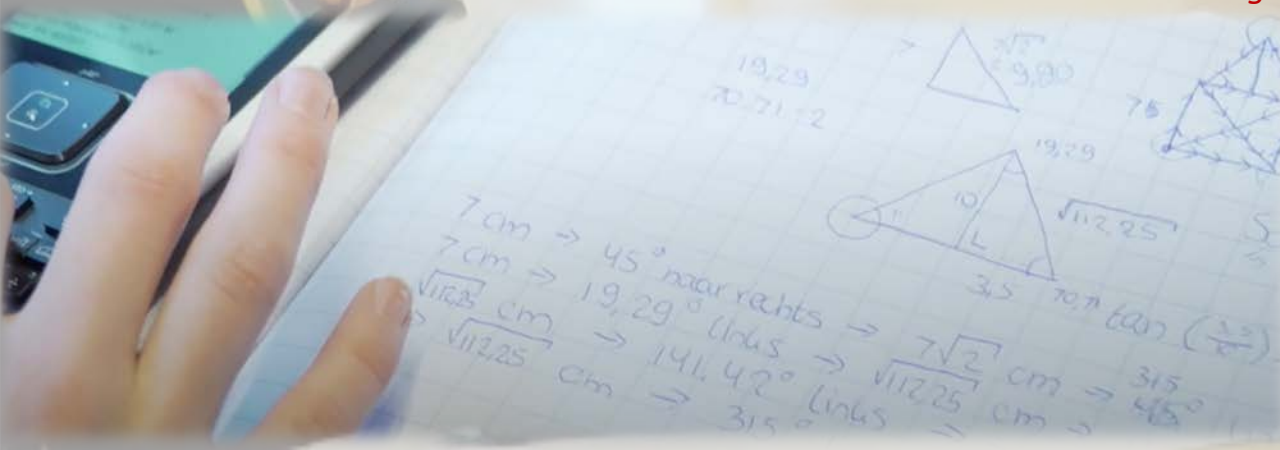
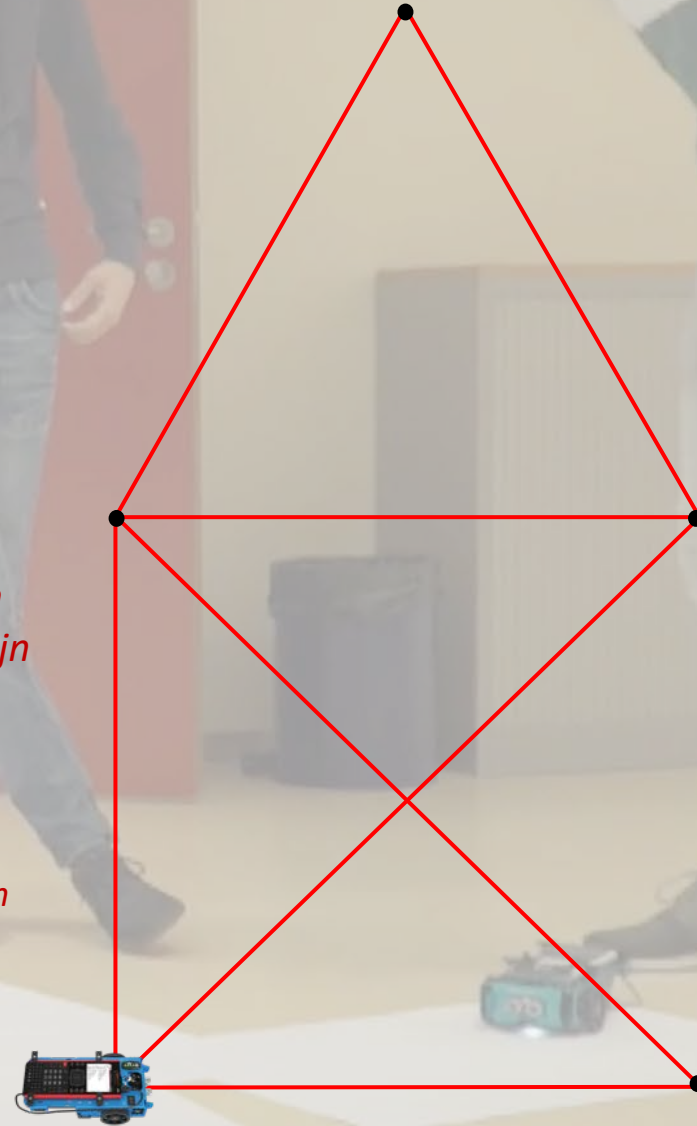
Meten van hoeken



Voor veel leerlingen is het een stimulans om te leren programmeren. De directe respons vinden ze leuk, het geeft een gevoel van beloning. Ze zijn heel fanatiek bezig met deze wiskundige activiteit, fanatieker dan met het maken van wiskundesommetjes!

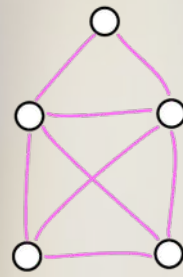
Bert Wikkerink
Docent Wiskunde
CSG Ludger Drachten

www.t3nederland.nl/nl/t3-europe/edublogs



Problem Solving

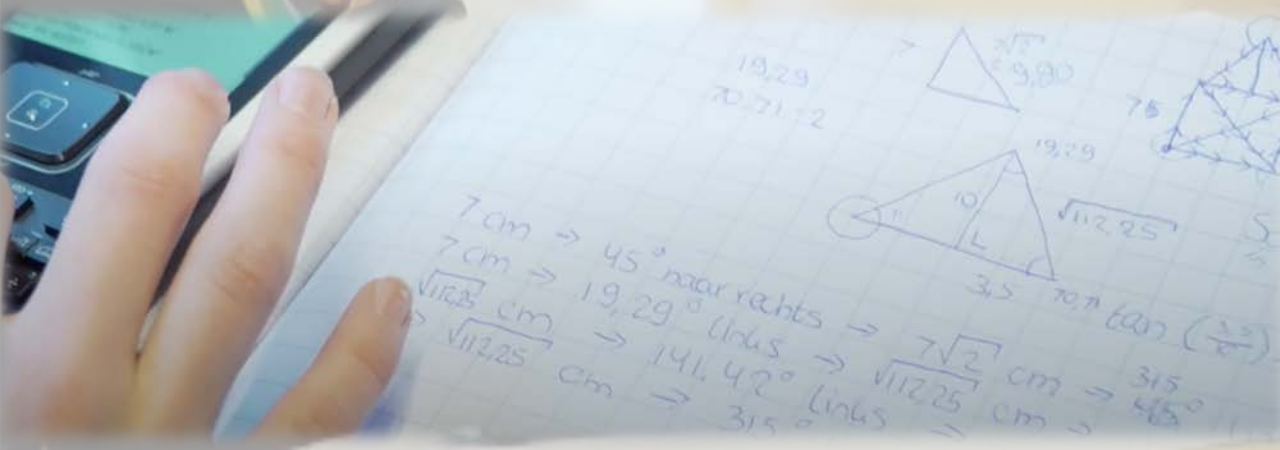
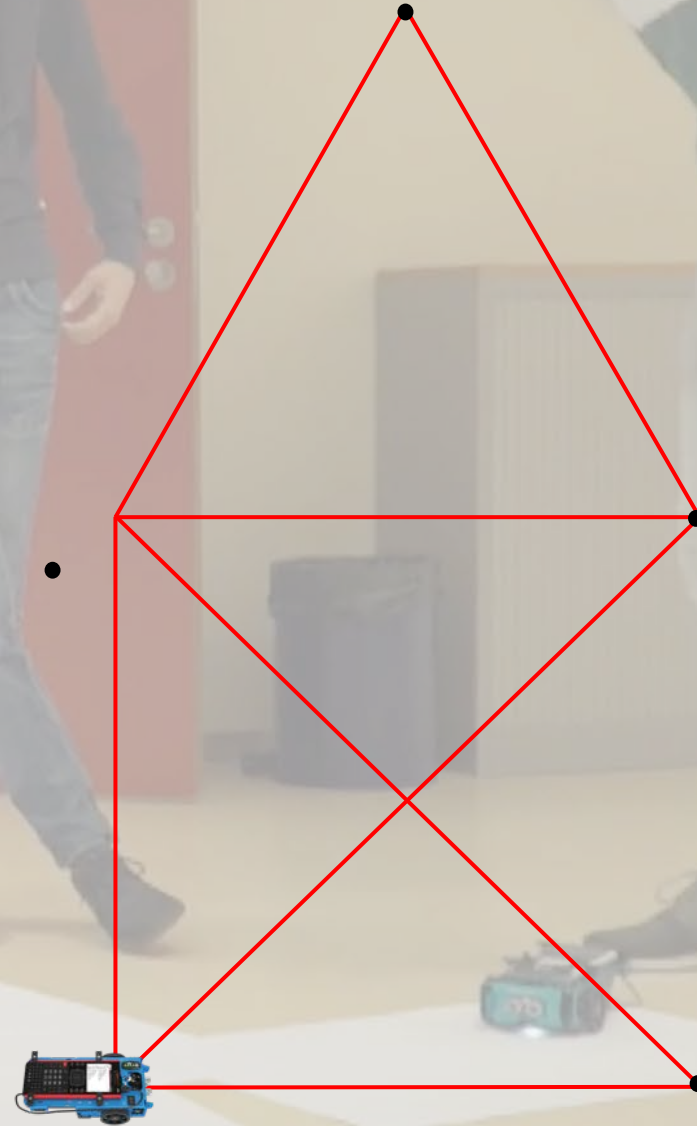
Meten van hoeken



Deze projecten sluiten mooi aan bij het wiskundeonderwijs. Leerlingen vragen wel eens wat is wiskunde en waar heb ik dat voor nodig? Nou hier zie je een hele mooie verbinding tussen wiskunde en de werkelijkheid, waardoor het leereffect groter is."

Ina Everts
Locatiedirecteur

www.t3nederland.nl/nl/t3-europe/edublogs



Problem Solving

Eenparig rechtlijnige beweging

```
import ti_rover as rv
a=rv.ranger_measurement()
alist=[]
rv.forward(100)
while a>0.1:
    a=rv.ranger_measurement()
    alist=alist+a
```

→ alist (python)

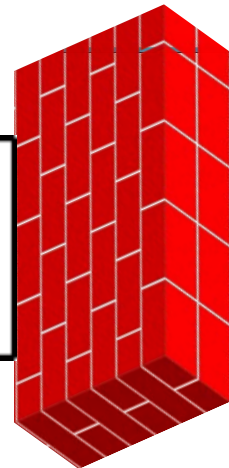
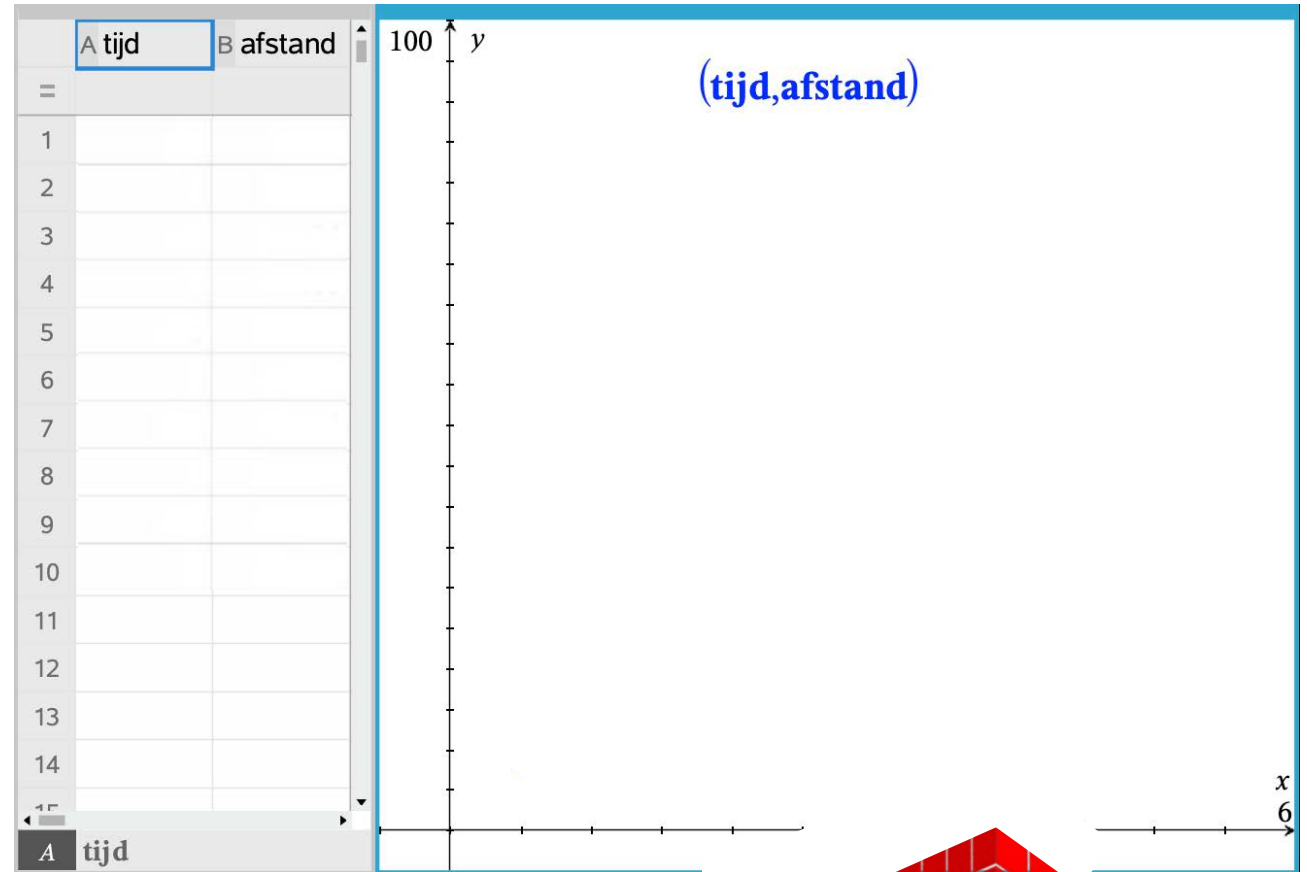
```
from ti_system import *
store_list("afstand",alist)
```

TI-Nspire var Python var

```
from time import *
t=localtime()
h=localtime()[3]
m=localtime()[4]
s=localtime()[5]
```

(2020, 6, 20, 12, 34, 49, 5, 172, 1)

→ tijd (TI-Nspire)



Problem Solving

Eenparig rechtlijnige beweging

```
import ti_rover as rv
a=rv.ranger_measurement()
alist=[]
rv.forward(100)
while a>0.1:
    a=rv.ranger_measurement()
    alist=alist+a
```

→ alist (python)

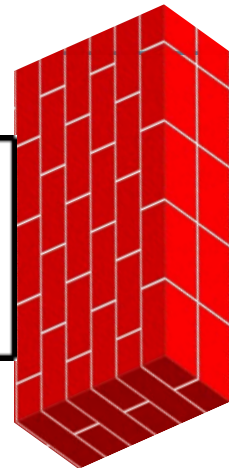
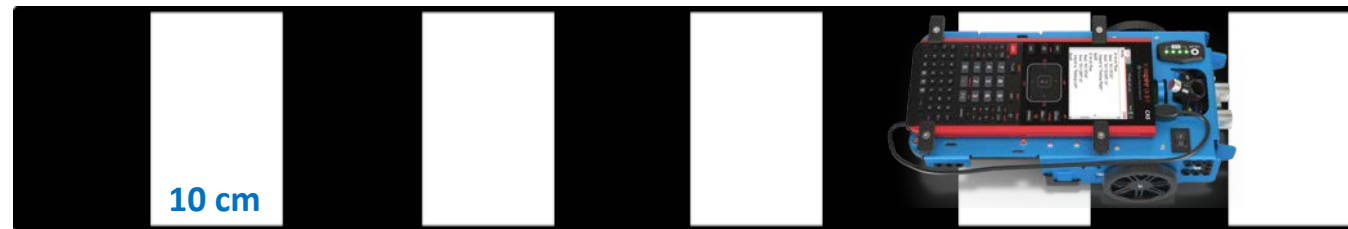
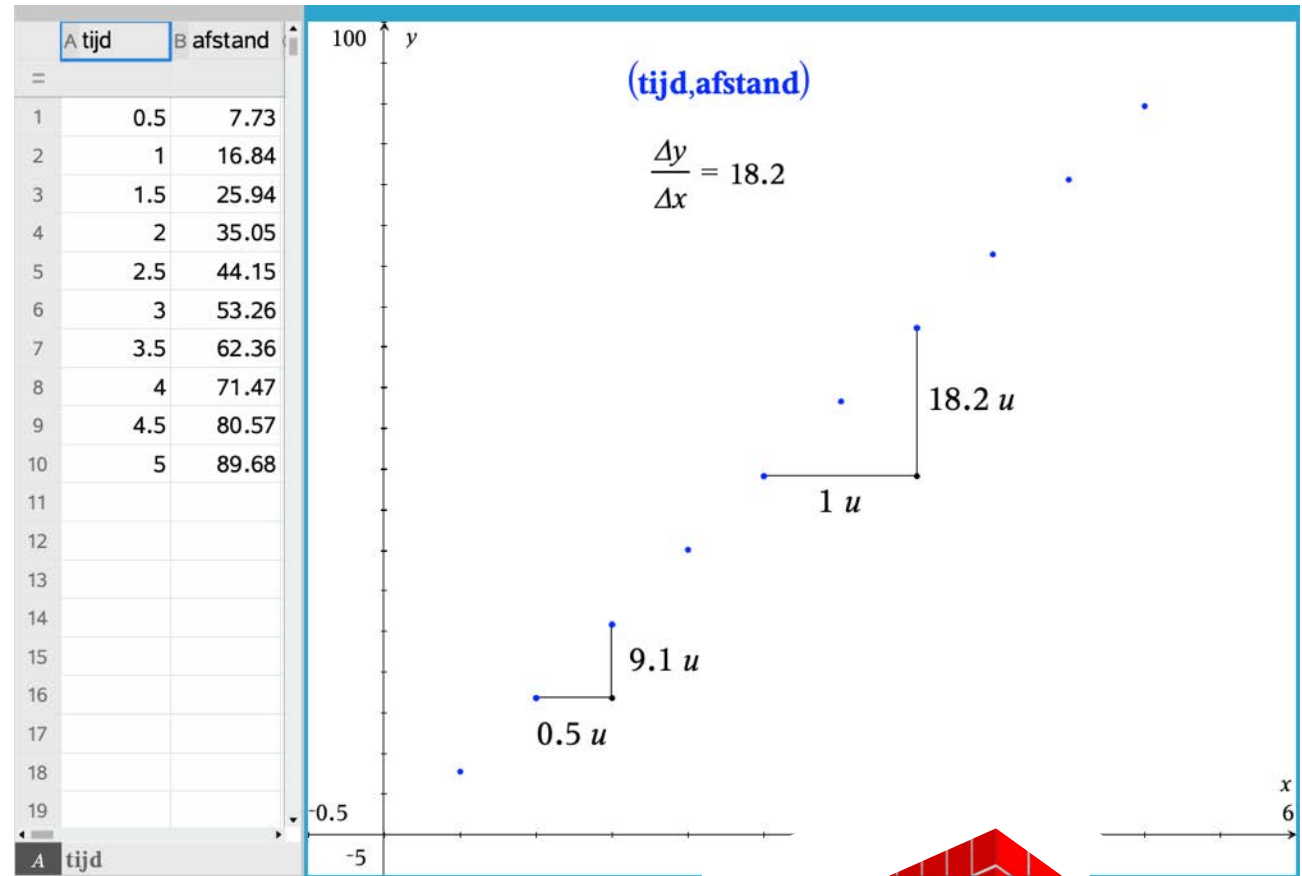
```
from ti_system import *
store_list("afstand",alist)
```

TI-Nspire var Python var

```
from time import *
t=localtime()
h=localtime()[3]
m=localtime()[4]
s=localtime()[5]
```

(2020, 6, 20, 12, 34, 49, 5, 172, 1)

→ tijd (TI-Nspire)



Problem Solving

Eenparig rechtlijnige beweging

```
import ti_rover as rv
a=rv.ranger_measurement()
alist=[]
rv.forward(100)
while a>0.1:
    a=rv.ranger_measurement()
    alist=alist+a
```

→ alist (python)

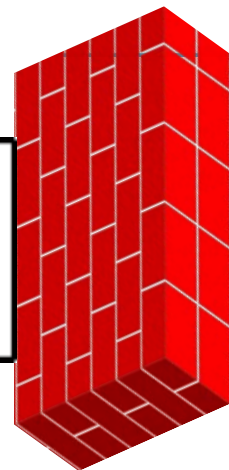
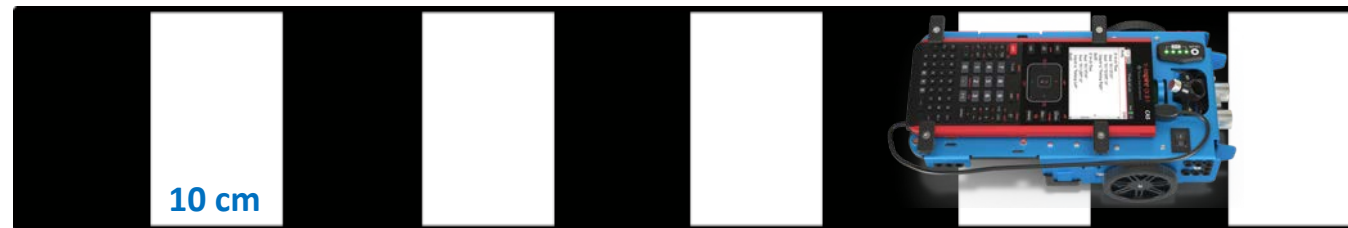
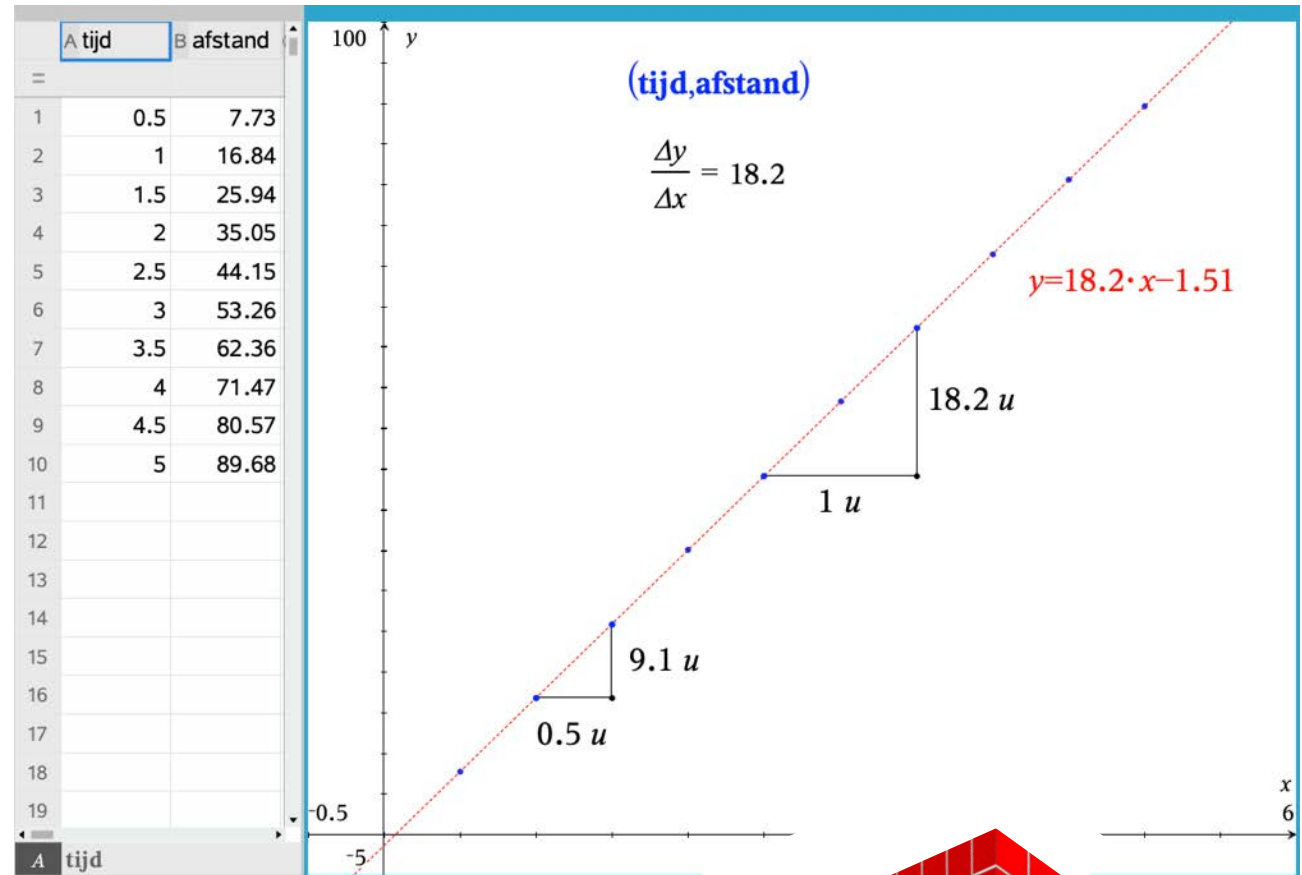
```
from ti_system import *
store_list("afstand",alist)
```

TI-Nspire var Python var

```
from time import *
t=localtime()
h=localtime()[3]
m=localtime()[4]
s=localtime()[5]
```

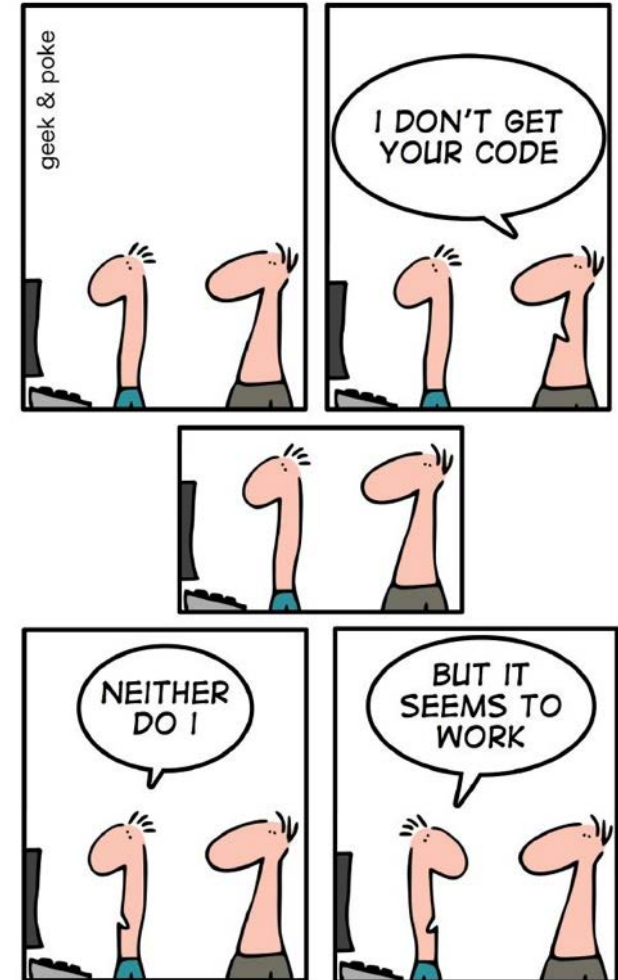
(2020, 6, 20, 12, 34, 49, 5, 172, 1)

→ tijd (TI-Nspire)



Programmeren

- Programmeren motiveert leerlingen abstracte concepten te onderzoeken!
- Programmeren stimuleert leerlingen tot het creatief oplossen van problemen!
- Programmeren geeft leerlingen een beter beeld van de hun omringde digitale wereld!

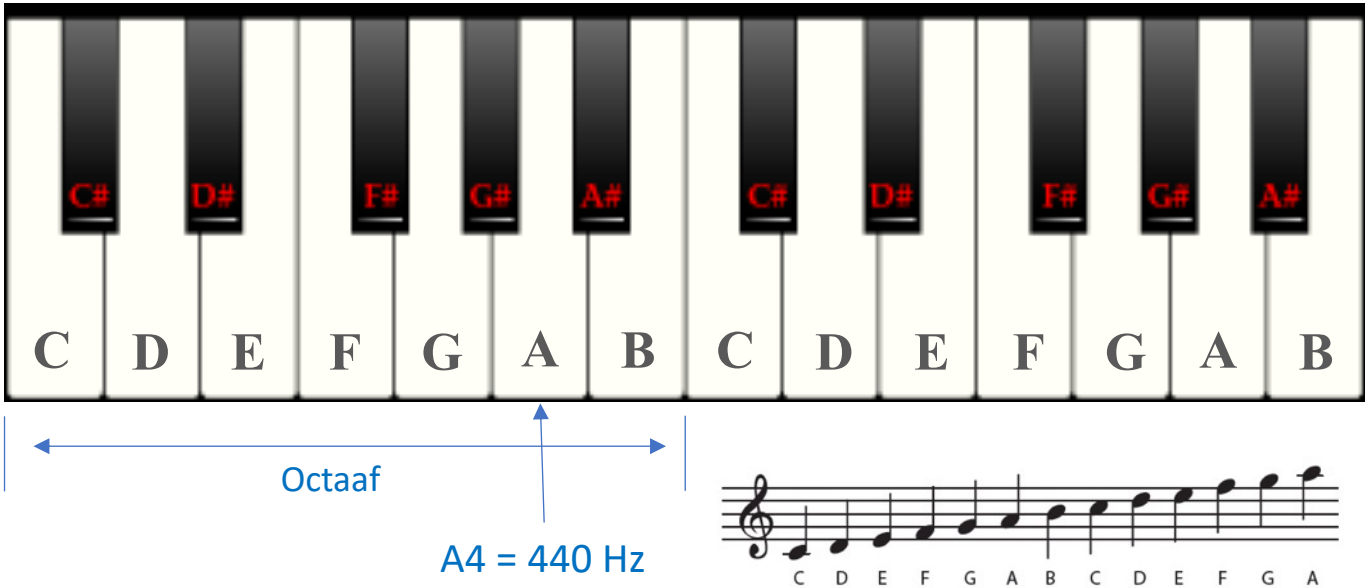


STEM PROJECTEN

Geluid



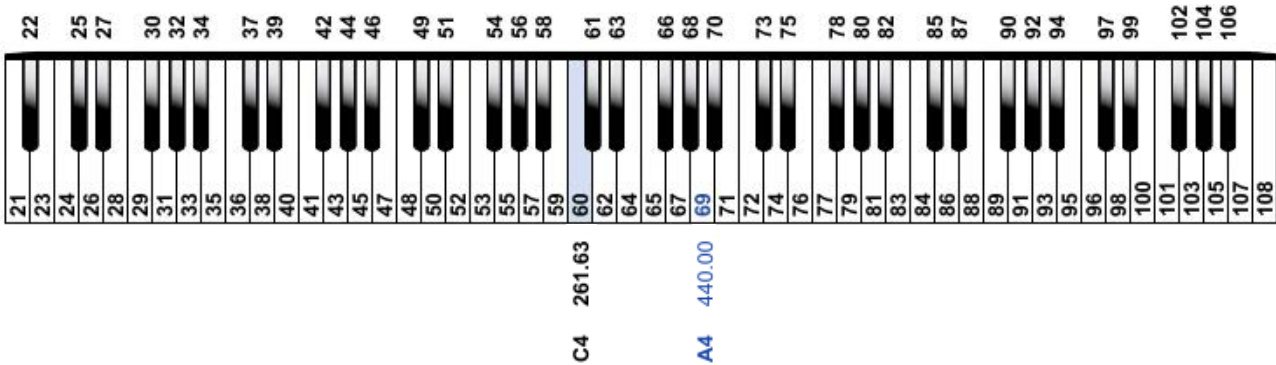
Voor ons oor is de afstand
tussen 220 Hz en 440 Hz gelijk aan
de afstand tussen 110 Hz en 220 Hz,
een octaaf.



Het MIDI-getal (Musical Instrument Digital Interface) voor A4 is 69.

Verband frequentie en MIDI-getallen

$$p = 69 + \log_2 \frac{f}{440} \cdot 12$$



Frequentie vs toonhoogte

toon	0	1	2	3	4	5	6	7	8	9
C	16,35	32,7	65,4	130,8	261,6	523,2	1046	2093	4186	8372
C#	17,32	34,64	69,29	138,5	277,1	554,3	1108	2217	4434	8869
D	18,35	36,7	73,41	146,8	293,6	587,3	1174	2349	4698	9397
D#	19,44	38,89	77,78	155,5	311,1	622,2	1244	2489	4978	9956
E	20,6	41,2	82,4	164,8	329,6	659,2	1318	2637	5274	10548
F	21,82	43,65	87,3	174,6	349,2	698,4	1396	2793	5587	11175
F#	23,12	46,24	92,49	184,9	369,9	739,9	1479	2959	5919	11839
G	24,49	48,99	97,99	195,9	391,9	783,9	1567	3135	6271	12543
G#	25,95	51,91	103,8	207,6	415,3	830,6	1661	3322	6644	13289
A	27,5	55	110	220	440	880	1760	3520	7040	14080
A#	29,13	58,27	116,5	233	466,1	932,3	1864	3729	7458	14917
B	30,86	61,73	123,4	246,9	493,8	987,7	1975	3951	7902	15804

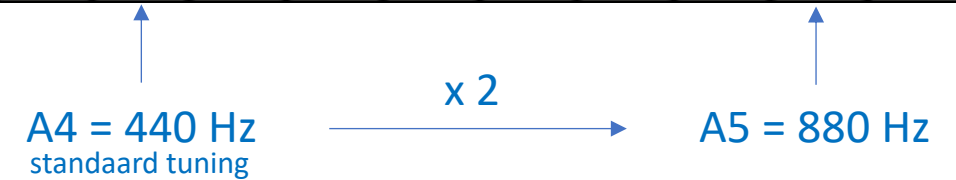
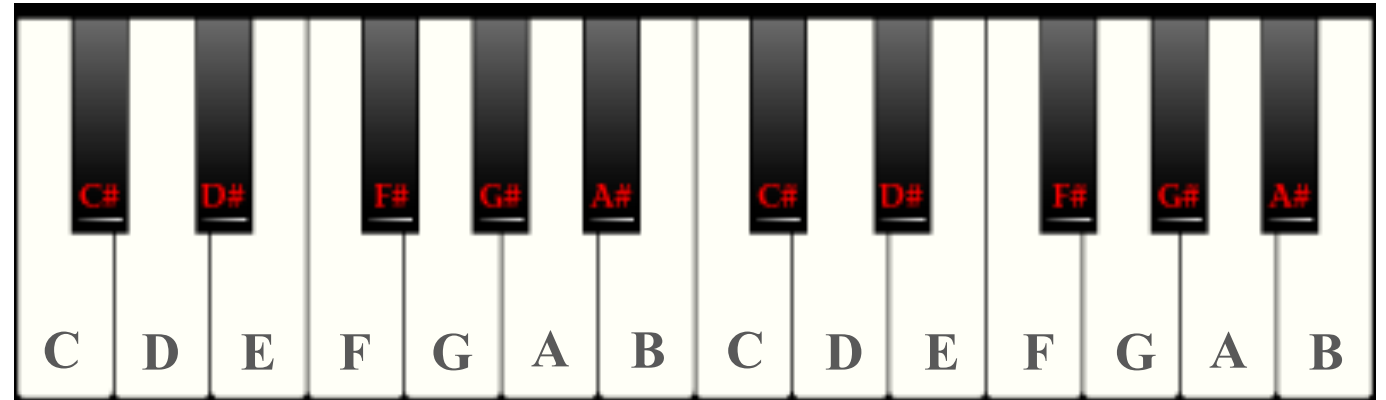
STEM PROJECTEN

Geluid



De toonafstand tussen naastliggende tonen is even groot.
Deze verhouding is gelijk aan $2^{\frac{1}{12}} = 1,05946309$.

- A#4 is 1 semitoon hoger dan A4 – $A\#4 = 440 \cdot 2^{\frac{1}{12}} = 466.1$ Hz
- B4 is 2 semitonen hoger dan A4 – $B4 = 440 \cdot 2^{\frac{2}{12}} = 493.8$ Hz
- A5 is 12 semitonen hoger dan A4 – $A5 = 440 \cdot 2^{\frac{12}{12}} = 880$ Hz



Frequentie vs toonhoogte

De toonafstand tussen naastliggende tonen is even groot.
Deze verhouding is gelijk aan $2^{\frac{1}{12}} = 1,05946309$.

- A#4 is 1 semitoon hoger dan A4 – $A\#4 = 440 \cdot 2^{\frac{1}{12}} = 466.1$ Hz
- B4 is 2 semitonen hoger dan A4 – $B4 = 440 \cdot 2^{\frac{2}{12}} = 493.8$ Hz
- A5 is 12 semitonen hoger dan A4 – $A5 = 440 \cdot 2^{\frac{12}{12}} = 880$ Hz

STEM PROJECTEN

Geluid

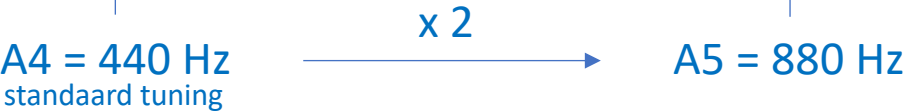
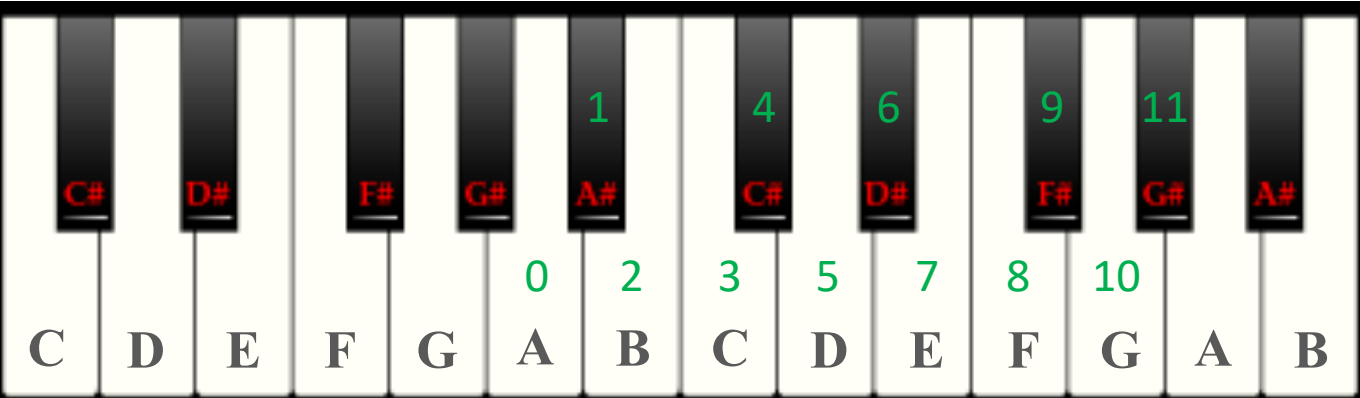


De toonafstand tussen naastliggende tonen is even groot.
Deze verhouding is gelijk aan $2^{\frac{1}{12}} = 1,05946309$.

- A#4 is 1 semitoon hoger dan A4 – $A\#4 = 440 \cdot 2^{\frac{1}{12}} = 466.1 \text{ Hz}$
- B4 is 2 semitonen hoger dan A4 – $B4 = 440 \cdot 2^{\frac{2}{12}} = 493.8 \text{ Hz}$
- A5 is 12 semitonen hoger dan A4 – $A5 = 440 \cdot 2^{\frac{12}{12}} = 880 \text{ Hz}$

$$f = 440 \cdot 2^{\frac{n}{12}} \longrightarrow$$

	n	f
A	0	440.
A#	1	466.164
B	2	493.883
C	3	523.251
C#	4	554.365
D	5	587.33
D#	6	622.254
E	7	659.255
F	8	698.456
F#	9	739.989
G	10	783.991
G#	11	830.609



Frequentie vs toonhoogte

De toonafstand tussen naastliggende tonen is even groot.
Deze verhouding is gelijk aan $2^{\frac{1}{12}} = 1,05946309$.

- A#4 is 1 semitoon hoger dan A4 – $A\#4 = 440 \cdot 2^{\frac{1}{12}} = 466.1 \text{ Hz}$
- B4 is 2 semitonen hoger dan A4 – $B4 = 440 \cdot 2^{\frac{2}{12}} = 493.8 \text{ Hz}$
- A5 is 12 semitonen hoger dan A4 – $A5 = 440 \cdot 2^{\frac{12}{12}} = 880 \text{ Hz}$

STEM PROJECTEN

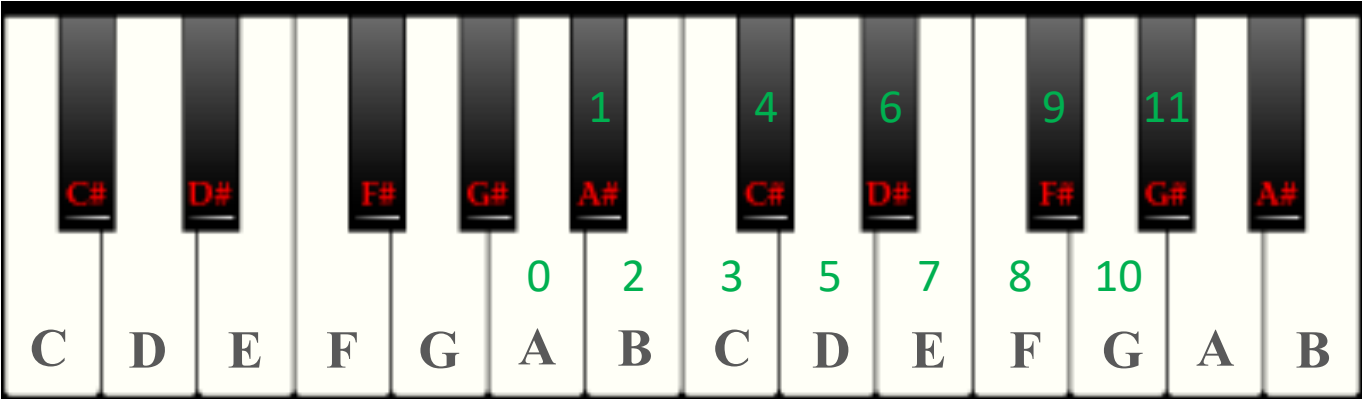
Geluid



 `geluid.py`
`from ti_hub import *`

```
sound.tone(440,1)  
sleep(1.5)
```

```
sound.note("A4",1)  
sleep(1.5)
```



$$f = 440 \cdot 2^{\frac{n}{12}}$$

A4 = 440 Hz
standaard tuning

x 2

A5 = 880 Hz

Frequentie vs toonhoogte

toon	0	1	2	3	4	5	6	7	8	9
C	16,35	32,7	65,4	130,8	261,6	523,2	1046	2093	4186	8372
C#	17,32	34,64	69,29	138,5	277,1	554,3	1108	2217	4434	8869
D	18,35	36,7	73,41	146,8	293,6	587,3	1174	2349	4698	9397
D#	19,44	38,89	77,78	155,5	311,1	622,2	1244	2489	4978	9956
E	20,6	41,2	82,4	164,8	329,6	659,2	1318	2637	5274	10548
F	21,82	43,65	87,3	174,6	349,2	698,4	1396	2793	5587	11175
F#	23,12	46,24	92,49	184,9	369,9	739,9	1479	2959	5919	11839
G	24,49	48,99	97,99	195,9	391,9	783,9	1567	3135	6271	12543
G#	25,95	51,91	103,8	207,6	415,3	830,6	1661	3322	6644	13289
A	27,5	55	110	220	440	880	1760	3520	7040	14080
A#	29,13	58,27	116,5	233	466,1	932,3	1864	3729	7458	14917
B	30,86	61,73	123,4	246,9	493,8	987,7	1975	3951	7902	15804

STEM PROJECTEN

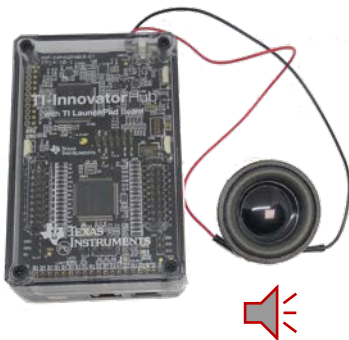
Geluid



```
geluid.py
from ti_hub import *
```

```
sound.tone(440,1)
sleep(1.5)
```

```
sound.note("A4",1)
sleep(1.5)
```

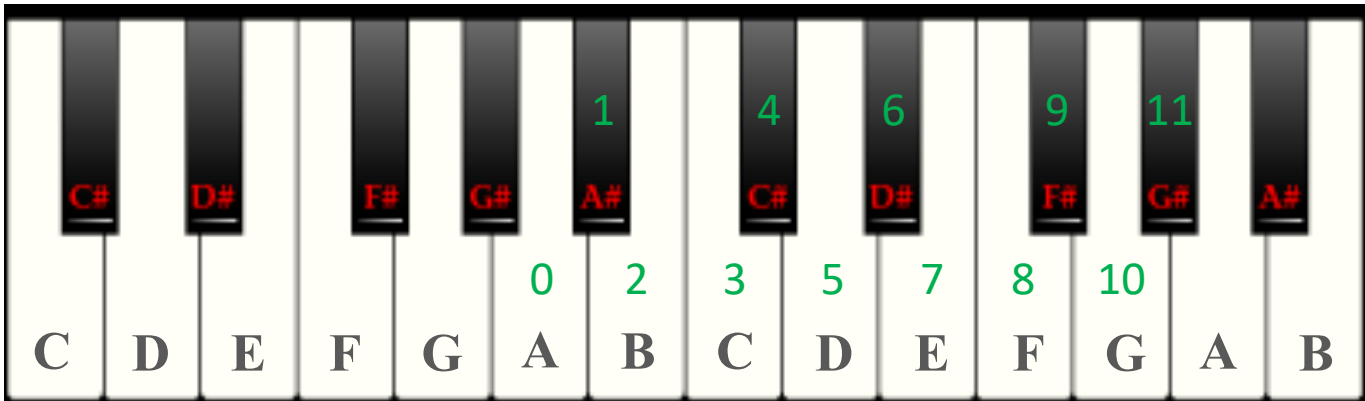


```
geluid.py
from ti_hub import *
```

```
vol=speaker("BB 1")
```

```
vol.tone(440,1)
sleep(1.5)
```

```
vol.note("A4",1)
sleep(1.5)
```



$$f = 440 \cdot 2^{\frac{n}{12}}$$

A4 = 440 Hz
standaard tuning

x 2

A5 = 880 Hz

Frequentie vs toonhoogte

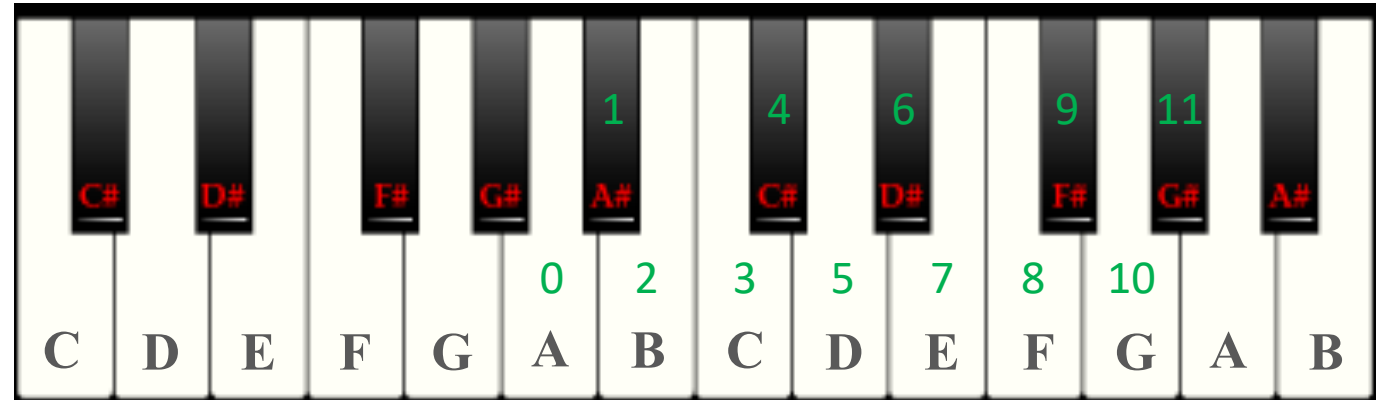
toon	0	1	2	3	4	5	6	7	8	9
C	16,35	32,7	65,4	130,8	261,6	523,2	1046	2093	4186	8372
C#	17,32	34,64	69,29	138,5	277,1	554,3	1108	2217	4434	8869
D	18,35	36,7	73,41	146,8	293,6	587,3	1174	2349	4698	9397
D#	19,44	38,89	77,78	155,5	311,1	622,2	1244	2489	4978	9956
E	20,6	41,2	82,4	164,8	329,6	659,2	1318	2637	5274	10548
F	21,82	43,65	87,3	174,6	349,2	698,4	1396	2793	5587	11175
F#	23,12	46,24	92,49	184,9	369,9	739,9	1479	2959	5919	11839
G	24,49	48,99	97,99	195,9	391,9	783,9	1567	3135	6271	12543
G#	25,95	51,91	103,8	207,6	415,3	830,6	1661	3322	6644	13289
A	27,5	55	110	220	440	880	1760	3520	7040	14080
A#	29,13	58,27	116,5	233	466,1	932,3	1864	3729	7458	14917
B	30,86	61,73	123,4	246,9	493,8	987,7	1975	3951	7902	15804

STEM PROJECTEN

Geluid

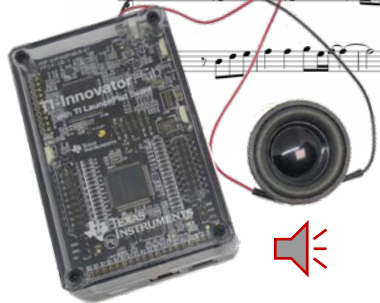


$$f = 440 \cdot 2^{\frac{n}{12}}$$



7 DAGEN LANG

Bots



	B	C noot	D tijd
=			
1	0	440.	0.125
2	3	523.251	0.125
3	5	587.33	0.125
4	7	659.255	0.25
5	7	659.255	0.25
6	8	698.456	0.125
7	5	587.33	0.125
8	7	659.255	0.5
9	-200	0.004229	0.125
10	5	587.33	0.125
11	5	587.33	0.0625
12	3	523.251	0.0625
13	2	493.883	0.125
14	3	523.251	0.25
15	0	440.	0.185
16	-2	391.995	0.185

$$C1 = 440 \cdot 2^{\frac{b1}{12}}$$

muziek.py

```
from ti_system import *
from ti_hub import *
```

```
noot=recall_list("noot")
tijd=recall_list("tijd")
```

```
vol=speaker("BB 1")
```

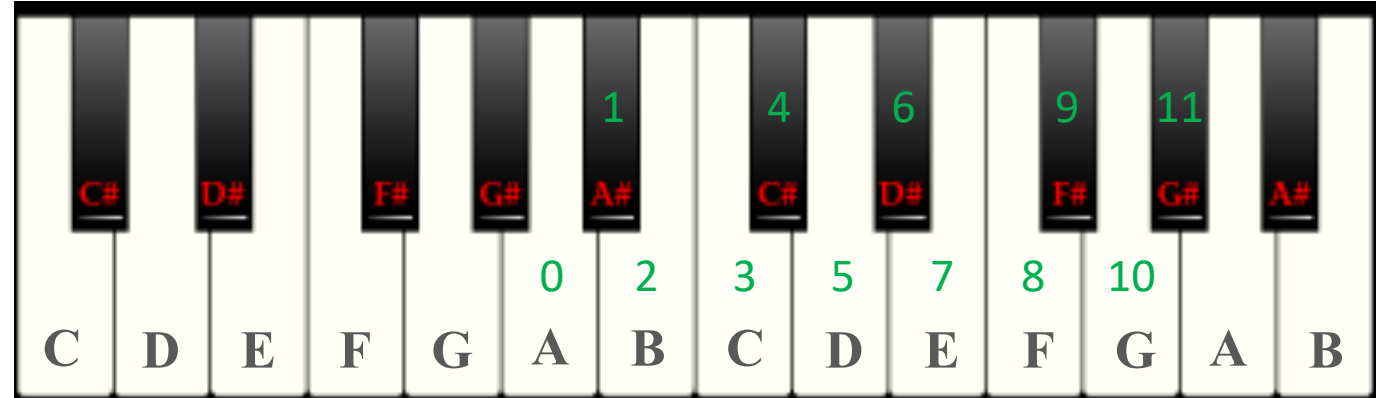
```
for i in range(len(noot)):
    vol.tone(noot[i],2*tijd[i])
    sleep(2*tijd[i])
```

STEM PROJECTEN

Geluid



$$f = 440 \cdot 2^{\frac{n}{12}}$$



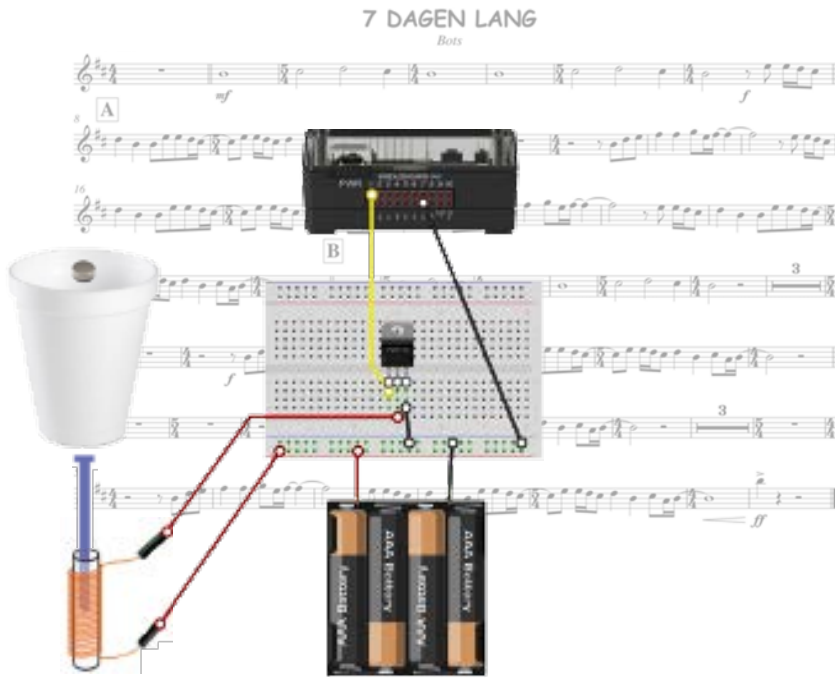
	B	C noot	D tijd
=			
1	0	440.	0.125
2	3	523.251	0.125
3	5	587.33	0.125
4	7	659.255	0.25
5	7	659.255	0.25
6	8	698.456	0.125
7	5	587.33	0.125
8	7	659.255	0.5
9	-200	0.004229	0.125
10	5	587.33	0.125
11	5	587.33	0.0625
12	3	523.251	0.0625
13	2	493.883	0.125
14	3	523.251	0.25
15	0	440.	0.185
16	-2	391.995	0.185

```
muziek.py
from ti_system import *
from ti_hub import *

noot=recall_list("noot")
tijd=recall_list("tijd")

vol=speaker("BB 1")

for i in range(len(noot)):
    vol.tone(noot[i],2*tijd[i])
    sleep(2*tijd[i])
```



STEM PROJECTEN

Pet Car Alarm

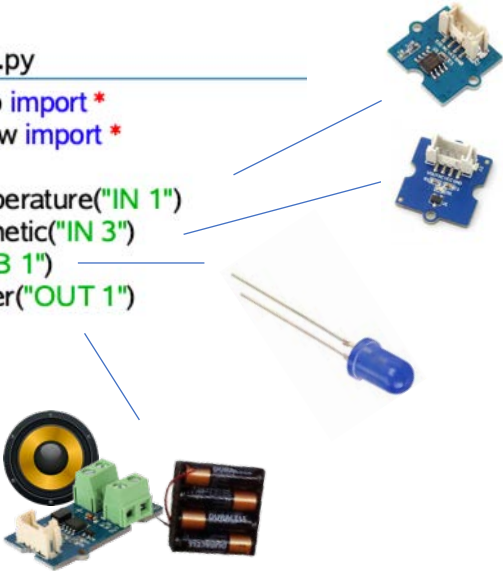


Onderzoek de wetenschap achter het broeikaseffect en gebruik wiskunde, programmeren en engineering voor het bouwen van een smart warmte auto-alarm.

alarm.py

```
from ti_hub import *
from ti_draw import *

temp=temperature("IN 1")
mag=magnetic("IN 3")
led=led("BB 1")
vol=speaker("OUT 1")
```



Conversie Farenheit ↔ Celcius!

Estimated Vehicle Interior Air Temperature v. Elapsed Time						
Elapsed time	Outside Air Temperature (F)					
	70	75	80	85	90	95
0 minutes	70	75	80	85	90	95
10 minutes	89	94	99	104	109	114
20 minutes	99	104	109	114	119	124
30 minutes	104	109	114	119	124	129
40 minutes	108	113	118	123	128	133
50 minutes	111	116	121	126	131	136
60 minutes	113	118	123	128	133	138
> 1 hour	115	120	125	130	135	140

Courtesy Jan Null, CCM; Department of Geosciences, San Francisco State University

STEM PROJECTEN

Pet Car Alarm

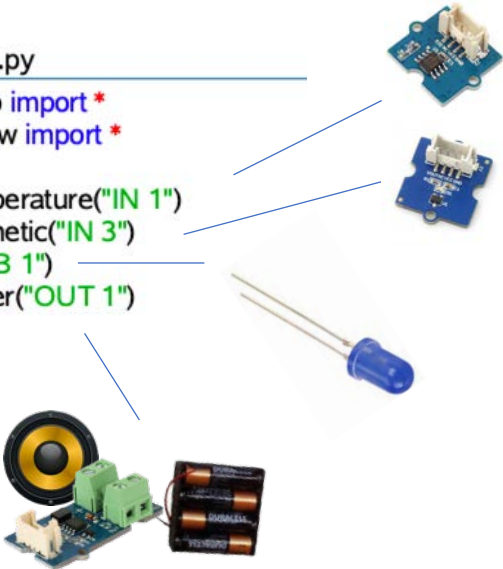


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alarm.py

```
from ti_hub import *
from ti_draw import *
```

```
temp=temperature("IN 1")
mag=magnetic("IN 3")
led=led("BB 1")
vol=speaker("OUT 1")
```



```
while get_key() != "esc":
    clear()
    t=round(temp.measurement(),1)
    m=mag.measurement()
```

Conversie Farenheit ↔ Celcius!

Estimated Vehicle Interior Air Temperature v. Elapsed Time						
Elapsed time	Outside Air Temperature (F)					
	70	75	80	85	90	95
0 minutes	70	75	80	85	90	95
10 minutes	89	94	99	104	109	114
20 minutes	99	104	109	114	119	124
30 minutes	104	109	114	119	124	129
40 minutes	108	113	118	123	128	133
50 minutes	111	116	121	126	131	136
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> 1 hour	115	120	125	130	135	140

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STEM PROJECTEN

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```
temp=temperature("IN 1")
mag=magnetic("IN 3")
led=led("BB 1")
vol=speaker("OUT 1")
```

```
while get_key() != "esc":
    clear()
    t=round(temp.measurement(),1)
    m=mag.measurement()
```

```
set_color(0,0,255)
draw_text(50,80,"HEATH CAR ALARM")
set_color(0,0,0)
draw_text(50,120,"Temperature inside car = {}".format(t))

if m<100:
    draw_text(50,100,"Baby in car")
else:
    draw_text(50,100,"Baby not in car")

if t>30 and m<100:
    set_color(255,0,0)
    draw_text(50,140,"Warning! Baby in heat distress")
    led.blink(10,1)
    vol.tone(440,1)
    sleep(0.5)
    vol.tone(880,0.5)
    sleep(0.5)
else:
    set_color(0,100,0)
    draw_text(50,140,"No problems detected")
```

Conversie Farenheit ↔ Celcius!

Estimated Vehicle Interior Air Temperature v. Elapsed Time						
Elapsed time	Outside Air Temperature (F)					
	70	75	80	85	90	95
0 minutes	70	75	80	85	90	95
10 minutes	89	94	99	104	109	114
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30 minutes	104	109	114	119	124	129
40 minutes	108	113	118	123	128	133
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STEM PROJECTEN

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vol=speaker("OUT 1")
```

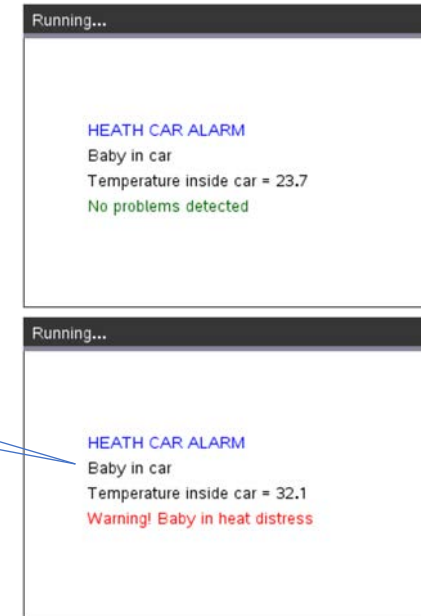
```
while get_key() != "esc":  
    clear()  
    t=round(temp.measurement(),1)  
    m=mag.measurement()
```

```
    set_color(0,0,255)  
    draw_text(50,80,"HEATH CAR ALARM")  
    set_color(0,0,0)  
    draw_text(50,120,"Temperature inside car = {}".format(t))  
  
    if m<100:  
        draw_text(50,100,"Baby in car")  
    else:  
        draw_text(50,100,"Baby not in car")  
  
    if t>30 and m<100:  
        set_color(255,0,0)  
        draw_text(50,140,"Warning! Baby in heat distress")  
        led.blink(10,1)  
        vol.tone(440,1)  
        sleep(0.5)  
        vol.tone(880,0.5)  
        sleep(0.5)  
    else:  
        set_color(0,100,0)  
        draw_text(50,140,"No problems detected")
```

Conversie Farenheit ↔ Celcius!

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0 minutes	70	75	80	85	90	95
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30 minutes	104	109	114	119	124	129
40 minutes	108	113	118	123	128	133
50 minutes	111	116	121	126	131	136
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STEM PROJECTEN

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    m=mag.measurement()
```

```
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set_color(0,0,0)
draw_text(50,120,"Temperature inside car = {}".format(t))

if m<100:
    draw_text(50,100,"Baby in car")
else:
    draw_text(50,100,"Baby not in car")

if t>30 and m<100:
    set_color(255,0,0)
    draw_text(50,140,"Warning! Baby in heat distress")
    led.blink(10,1)
    vol.tone(440,1)
    sleep(0.5)
    vol.tone(880,0.5)
    sleep(0.5)
else:
    set_color(0,100,0)
    draw_text(50,140,"No problems detected")
```

Conversie Farenheit ↔ Celcius!

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Elapsed time	Outside Air Temperature (F)					
	70	75	80	85	90	95
0 minutes	70	75	80	85	90	95
10 minutes	89	94	99	104	109	114
20 minutes	99	104	109	114	119	124
30 minutes	104	109	114	119	124	129
40 minutes	108	113	118	123	128	133
50 minutes	111	116	121	126	131	136
60 minutes	113	118	123	128	133	138
> 1 hour	115	120	125	130	135	140

Courtesy Jan Null, CCM; Department of Geosciences, San Francisco State University



OOP met Python

Wiskundige objecten

Everything is
an object
in Python



- ```
>>>n=193
>>>type(n)
<class 'int'>
>>>r=1.93
>>>type(r)
<class 'float'>
```
- ```
>>>lst=[1,2,3]
>>>type(lst)
<class 'list'>
>>>lst.append(4)
>>>lst
[1, 2, 3, 4]
```
- ```
>>>email="k-stulens@ti.com"
>>>type(email)
<class 'str'>
>>>email.upper()
'K-STULENS@TI.COM'
```



# OOP met Python

## Wiskundige objecten



\*circle.py

```
from math import *
from ti_draw import *
```

```
class Circle:
```

```
 def __init__(self, rad=10, xcoord=100, ycoord=100):
```

```
 self.rad=rad
```

```
 self.xcoord=xcoord
```

```
 self.ycoord=ycoord
```

```

```

```
 def __str__(self):
```

```
 return 'Circle with radius {} and center point ({}.{})'.format(self.rad, self.xcoord, self.ycoord)
```

```

```

```
 def getArea(self):
```

```
 return pi*self.rad**2
```

```

```

```
 def getCircumference(self):
```

```
 return 2*pi*self.rad
```

```

```

```
 def getCircle(self):
```

```
 draw_circle(self.xcoord, self.ycoord, self.rad)
```

} → Eigenschappen

} → Methoden

class = User Defined Object

Everything is  
an object  
in Python



- ```
>>>n=193
>>>type(n)
<class 'int'>
>>>r=1.93
>>>type(r)
<class 'float'>
```
- ```
>>>lst=[1,2,3]
>>>type(lst)
<class 'list'>
>>>lst.append(4)
>>>lst
[1, 2, 3, 4]
```
- ```
>>>email="k-stulens@ti.com"
>>>type(email)
<class 'str'>
>>>email.upper()
'K-STULENS@TI.COM'
```

OOP met Python

Wiskundige objecten

Everything is
an object
in Python



 *circle.py

```
from math import *
from ti_draw import *

class Circle:
    def __init__(self, rad=10, xcoord=100, ycoord=100):
        self.rad=rad
        self.xcoord=xcoord
        self.ycoord=ycoord
    def __str__(self):
        return 'Circle with radius {} and center point ({}.{})'.format(self.rad, self.xcoord, self.ycoord)
    def getArea(self):
        return pi*self.rad**2
    def getCircumference(self):
        return 2*pi*self.rad
    def getCircle(self):
        draw_circle(self.xcoord, self.ycoord, self.rad)
```

 Python Shell

```
>>> #Running circle.py
>>> from circle import *
>>> c=Circle(25,100,150)
>>> c.rad
25
>>> c.xcoord
100
>>> c.ycoord
150
>>> c.getArea()
1963.495408493621
>>> c.getCircumference()
157.0796326794897
>>>
```

OOP met Python

Wiskundige objecten

Everything is
an object
in Python



*circle.py

```
from math import *
from ti_draw import *

class Circle:
    def __init__(self, rad=10, xcoord=100, ycoord=100):
        self.rad=rad
        self.xcoord=xcoord
        self.ycoord=ycoord
    def __str__(self):
        return 'Circle with radius {} and center point ({} , {})' .format(self.rad, self.xcoord, self.ycoord)
    def getArea(self):
        return pi*self.rad**2
    def getCircumference(self):
        return 2*pi*self.rad
    def getCircle(self):
        draw_circle(self.xcoord, self.ycoord, self.rad)
```

Python Shell

```
>>>#Running circle.py
>>>from circle import *
>>>c=Circle(25,100,150)
>>>c.rad
25
>>>c.xcoord
100
>>>c.ycoord
150
>>>c.getArea()
1963.495408493621
>>>c.getCircumference()
157.0796326794897
>>>
>>>print(c)
Circle with radius 25 and center point (100,150)
>>>
```

OOP met Python

Wiskundige objecten

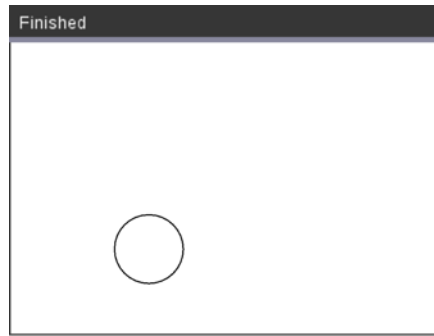
Everything is
an object
in Python



*circle.py

```
from math import *
from ti_draw import *

class Circle:
    def __init__(self, rad=10, xcoord=100, ycoord=100):
        self.rad=rad
        self.xcoord=xcoord
        self.ycoord=ycoord
    def __str__(self):
        return 'Circle with radius {} and center point ({}, {})'.format(self.rad, self.xcoord, self.ycoord)
    def getArea(self):
        return pi*self.rad**2
    def getCircumference(self):
        return 2*pi*self.rad
    def getCircle(self):
        draw_circle(self.xcoord, self.ycoord, self.rad)
```



Python Shell

```
>>> #Running circle.py
>>> from circle import *
>>> c=Circle(25,100,150)
>>> c.rad
25
>>> c.xcoord
100
>>> c.ycoord
150
>>> c.getArea()
1963.495408493621
>>> c.getCircumference()
157.0796326794897
>>>
>>> print(c)
Circle with radius 25 and center point (100,150)
>>>
>>> c.getCircle()
>>>
```



OOP met Python

Output (virtual) objecten

Everything is
an object
in Python



```
from ti_draw import *
from ti_image import *
from time import *

w,h = get_screen_dim()
hub_front=load_image("front_view")
front_x = w/2 - hub_front.w/2
front_y = h/2 - hub_front.h/2

class led():
    def __init__(self,port):
        self.img = load_image("led_t")
        self.dx = 82
        self.x_off = 68
        if port == "BB 1":
            self.x = self.x_off
        elif port == "BB 2":
            self.x = self.x_off+ self.dx
        elif port == "BB 3":
            self.x = self.x_off+ 2*self.dx
        self.y =160
        self.img.show_image(self.x,self.y)
        hub_front.show_image(0,0)

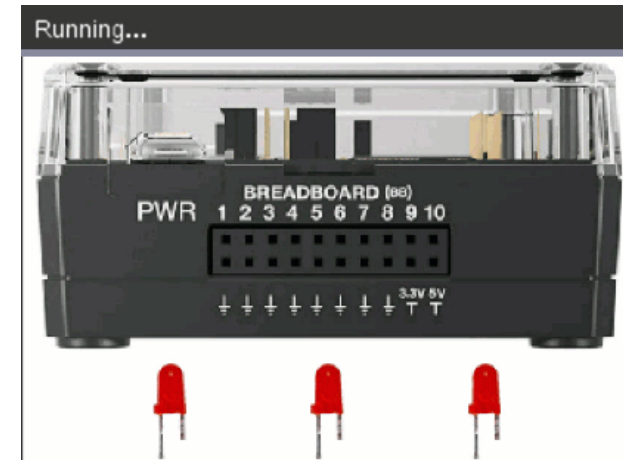
    def on (self):
        self.img.show_image(self.x,self.y)
        hub_front.show_image(front_x,0)
        set_color(255,0,150)
        fill_rect(self.x+3,self.y+5,13,20)
        fill_circle(self.x+9,self.y+6,6)

    def off (self):
        self.img.show_image(self.x,self.y)
        hub_front.show_image(front_x,0)
        hub_front.show_image(front_x,0)
        self.img.show_image(self.x,self.y)
```

```
leds=[]
```

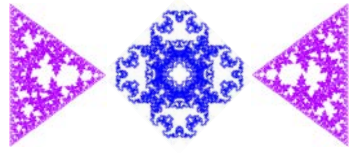
```
for n in range(3):
    leds.append (led('BB ' + str(n+1)))
```

```
while not escape():
    for aled in leds:
        aled.on()
        sleep_ms(250)
        aled.off()
        sleep_ms(250)
```



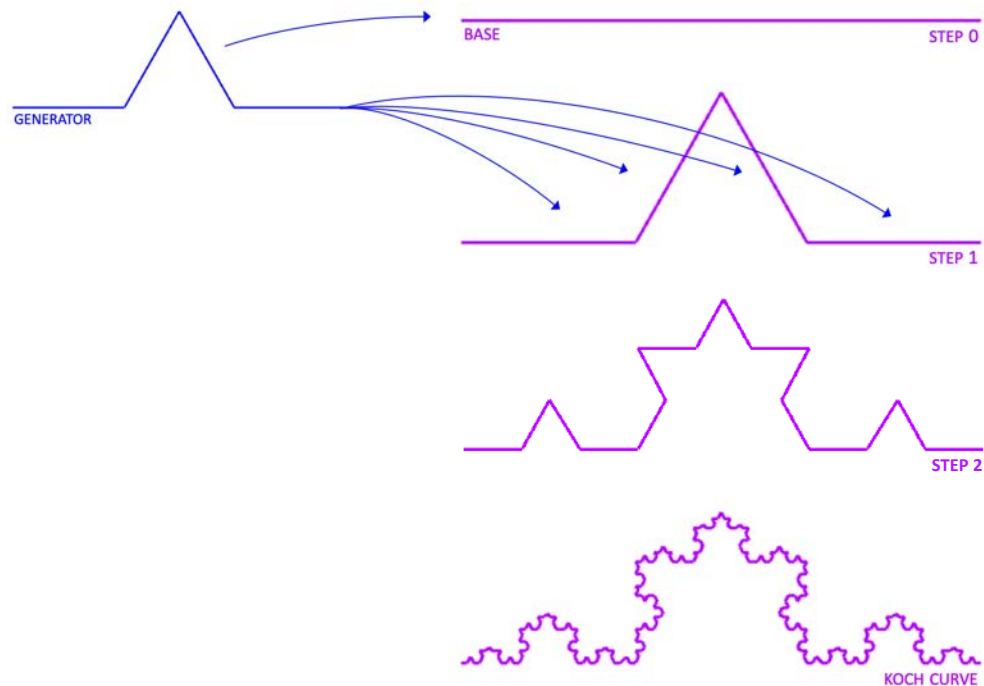
STEAM Projecten

Eigenaardige lineaire kronkels



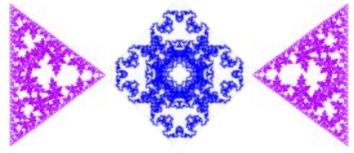
$$T : \begin{bmatrix} x \\ y \end{bmatrix} \mapsto \begin{bmatrix} a & -b \\ b & a \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} e \\ f \end{bmatrix}$$

T = a composition of a translation, rotation and a dilation



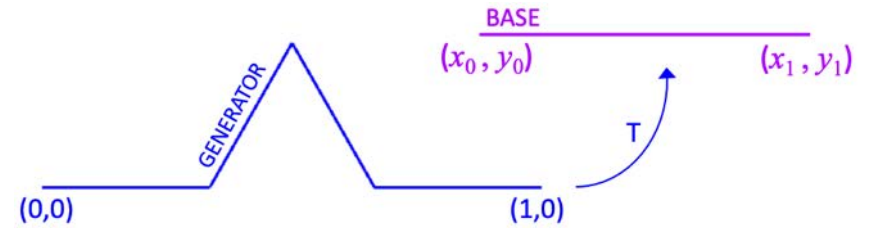
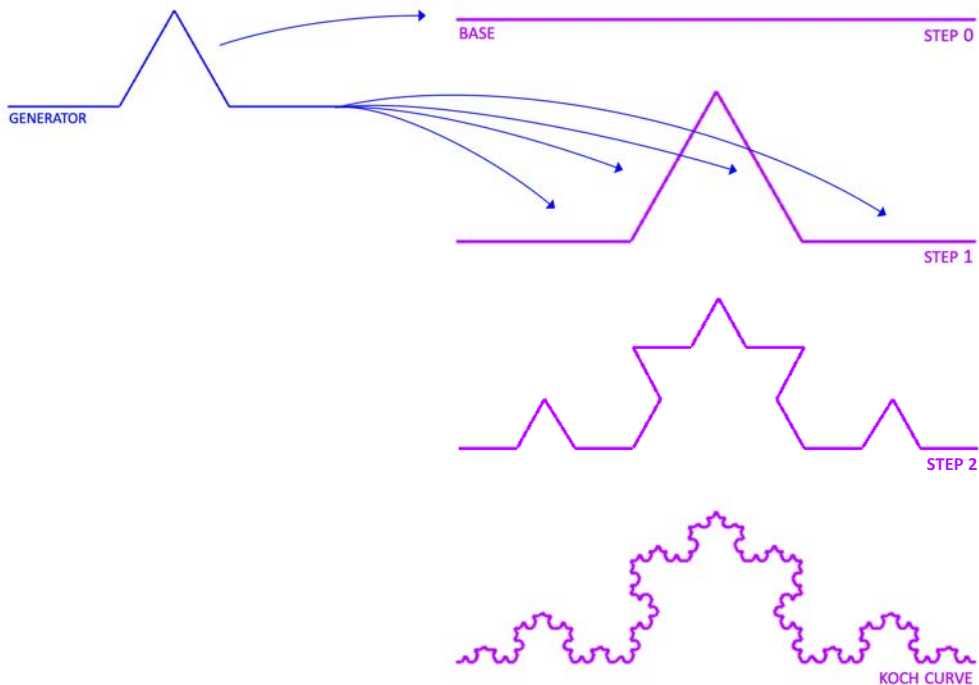
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Eigenaardige lineaire kronkels



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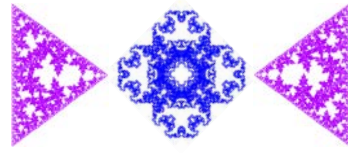
T = a composition of a translation, rotation and a dilation



$$T : \begin{bmatrix} x \\ y \end{bmatrix} \mapsto \begin{bmatrix} x_1 - x_0 & y_0 - y_1 \\ y_1 - y_0 & x_1 - x_0 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} x_0 \\ y_1 \end{bmatrix}$$

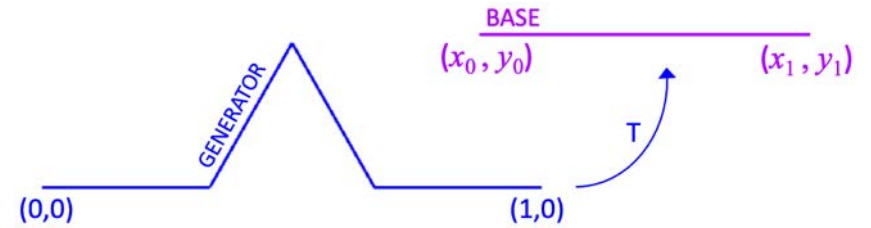
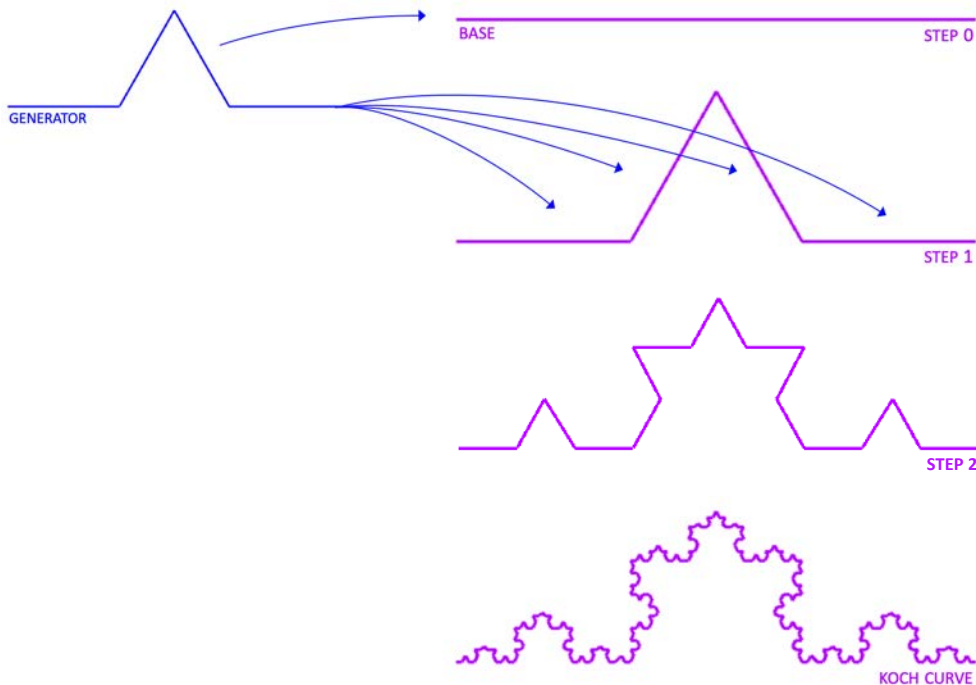
STEAM Projecten

Eigenaardige lineaire kronkels



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Fractal LinearTransformation based on segment [p1,p2]

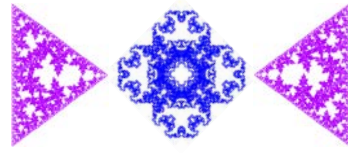
```
def transform(x,y,p1,p2):
```

```
    a=p2[0]-p1[0] ; b=p2[1]-p1[1] ; e=p1[0] ; f=p1[1]
```

```
    return [a*x-b*y+e,b*x+a*y+f]
```

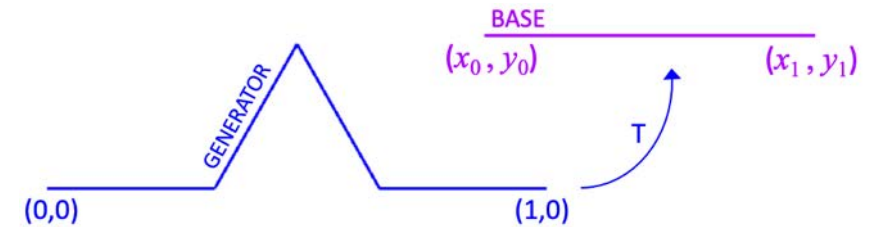
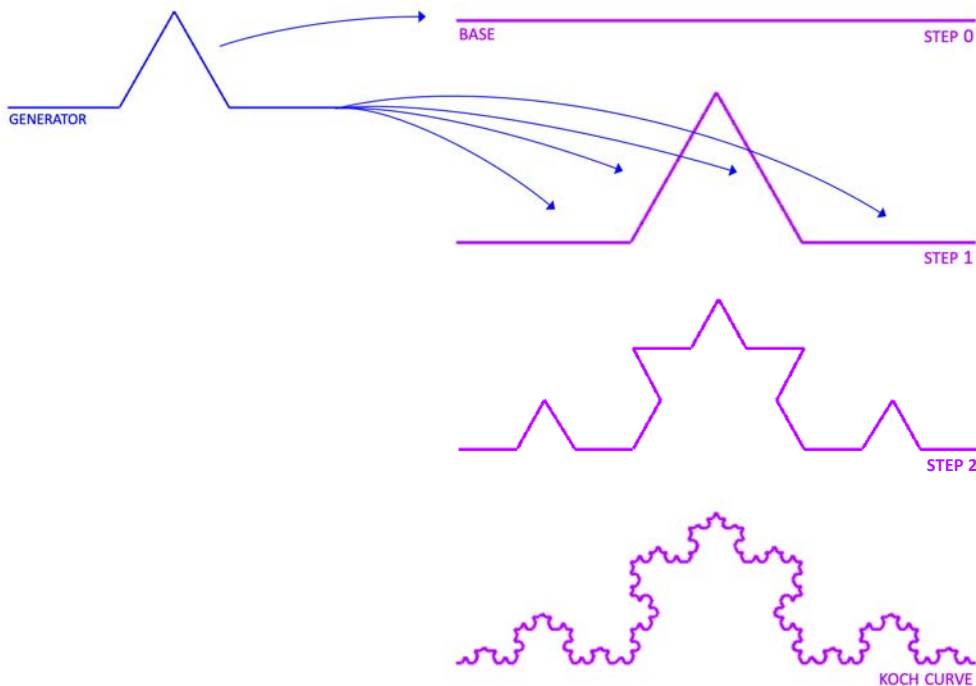
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Eigenaardige lineaire kronkels



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```

Fractal Points on segment [p1,p2]

```
def genpoints(p1,p2):
    points=[]
    for i in range(0,u):
        yield transform(xg[i],yg[i],p1,p2)
```

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Eigenaardige linaire kronkels

```
# Generate Fractal
v=len(xb)
```

```
for j in range(v-1):
    set_color(178,0,255)
    pb=[xb[j],yb[j]] ; pe=[xb[j+1],yb[j+1]]

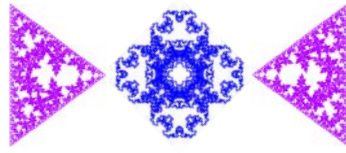
    # Draw Base - Generation 0
    if gen==0:
        draw_segment(pb[0],pb[1],pe[0],pe[1])
```

```
    # Define Fractal Generation
    elif gen>=1:
        fracgen=[[genpoints(pb,pe)]]
        for g in range(0,gen-1):
            fracgen.append([])
            for k in range(0,(u-1)**g):
                pe=next(fracgen[0][k])
                for i in range(0,u-1):
                    pb=pe.copy()
                    pe=next(fracgen[0][k])
                    fracgen[1].append(genpoints(pb,pe))
            fracgen.remove(fracgen[0])
```

```
    # Plot Fractal
    if gen>=1:
        for seg in range(0,(u-1)**(gen-1)):
            np=[]
            for i in range(0,u):
                np.append(next(fracgen[0][seg]))
            for j in range(0,u-1):
                draw_segment(np[j][0],np[j][1],np[j+1][0],np[j+1][1])
```

```
# Fractal LinearTransformation based on segment [p1,p2]
def transform(x,y,p1,p2):
    a=p2[0]-p1[0] ; b=p2[1]-p1[1] ; e=p1[0] ; f=p1[1]
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Eigenaardige linaire kronkels

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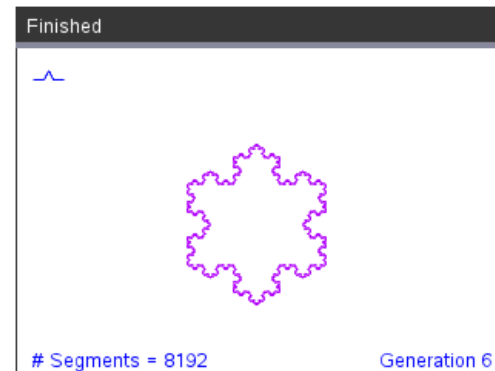
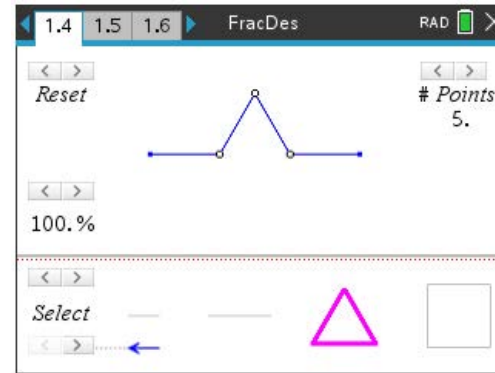
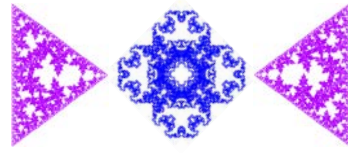
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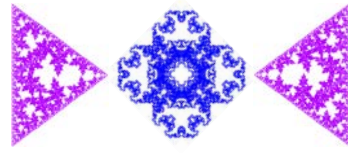
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Eigenaardige linaire kronkels



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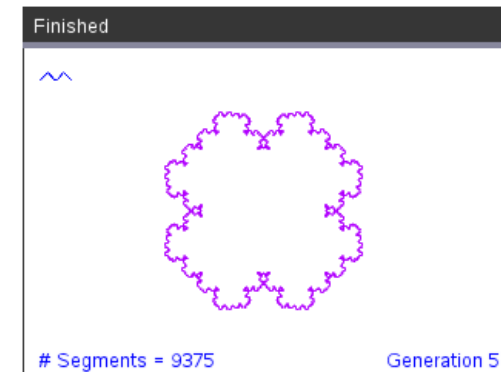
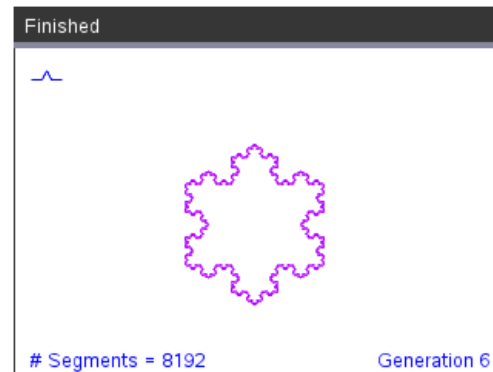
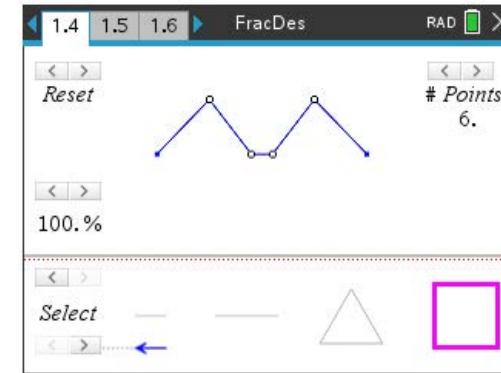
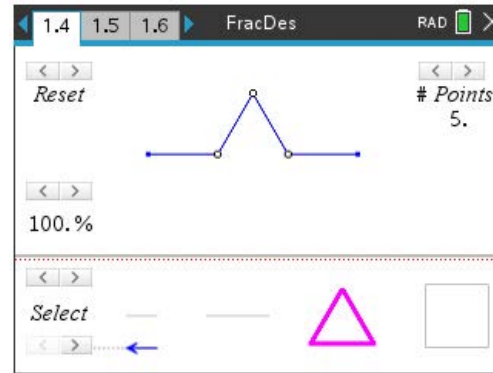
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Eigenaardige linaire kronkels

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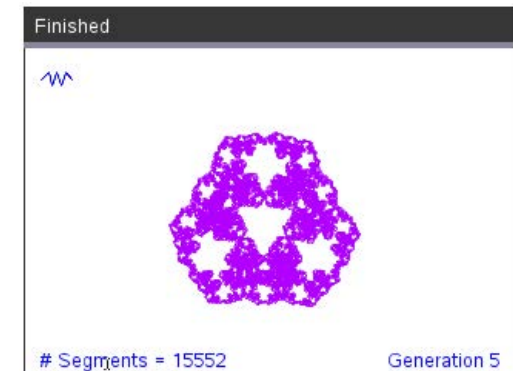
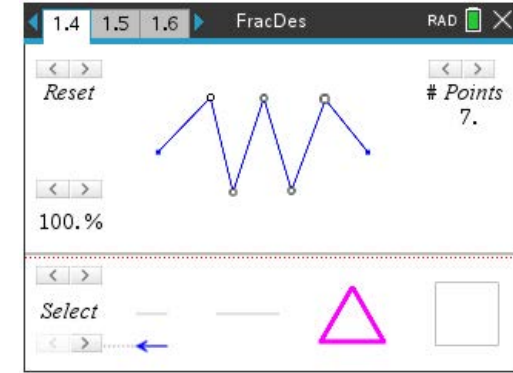
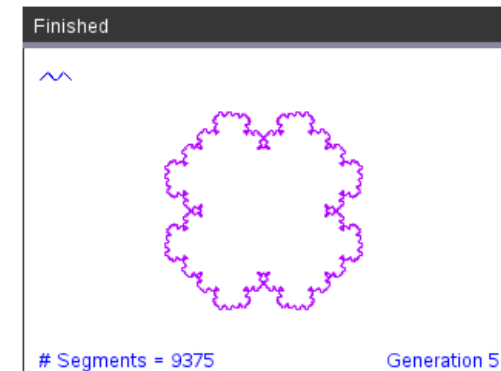
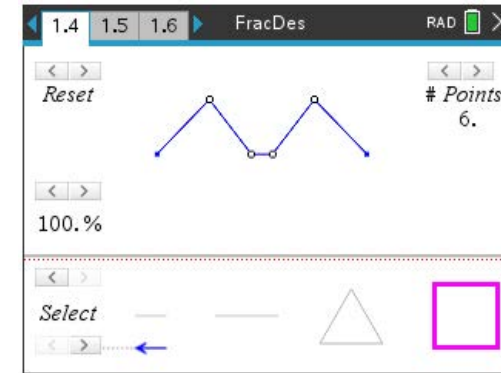
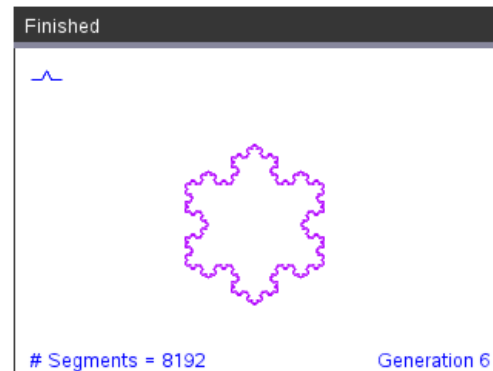
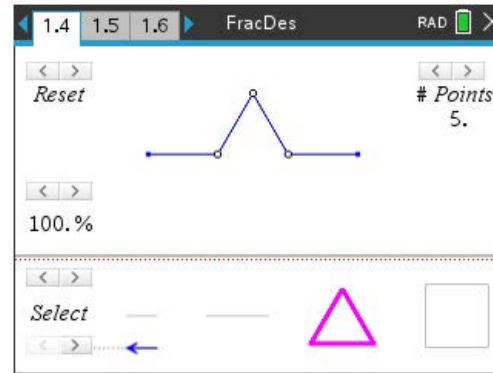
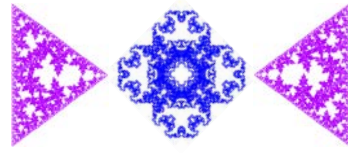
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Python in de klas

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Teaching is more than the dissemination of content

Teaching should cultivate curiosity and inquiry

Teaching should spark student imagination and creativity



Some skills become more important because technology requires it

Some skills become less important because technology replaces it

Some skills becomes possible because technology allows it



based on Bert Waits - 2000



TEXAS INSTRUMENTS